

11. Kosmologietag

# Vacuum Selection on Axionic Landscapes

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In collaboration with:  
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# Motivation

- **Multifield** inflation appear generic in String Theory.
- The concrete construction is unknown.
- Create large numbers of **random landscapes** and investigate their statistical properties.
- Can we identify **generic features** of inflation on random landscapes?

D. Battefeld, T. Battefeld, S. Schulz 2012

# Questions

- How likely is Inflation in a random potential?
- Duration of inflation? Distribution of number of efoldings?
- How do the answers change with increasing randomness?
- What is the type of Inflation?
- Distribution of Minima, Maxima, Saddles?

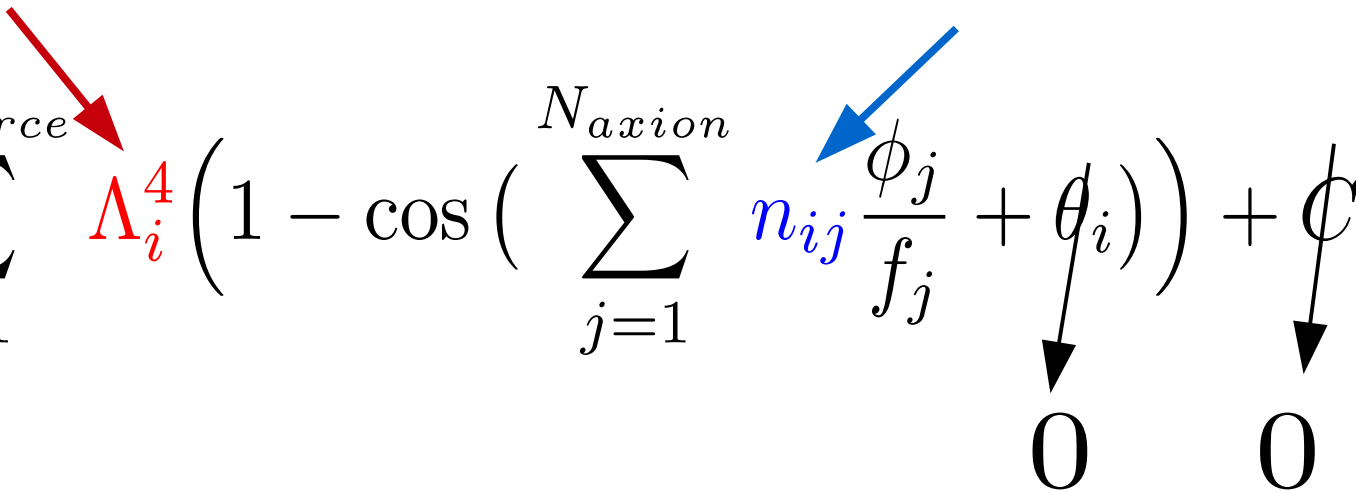
T. Higaki, F. Takahashi 2014

- Where is the final resting place dynamical evolution on the potential?

# Axionic potential

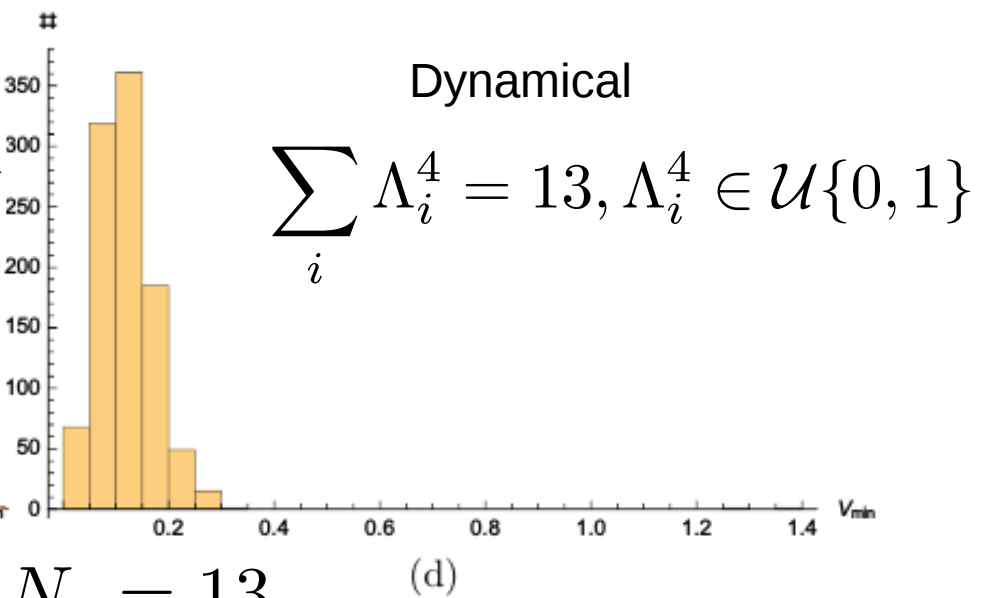
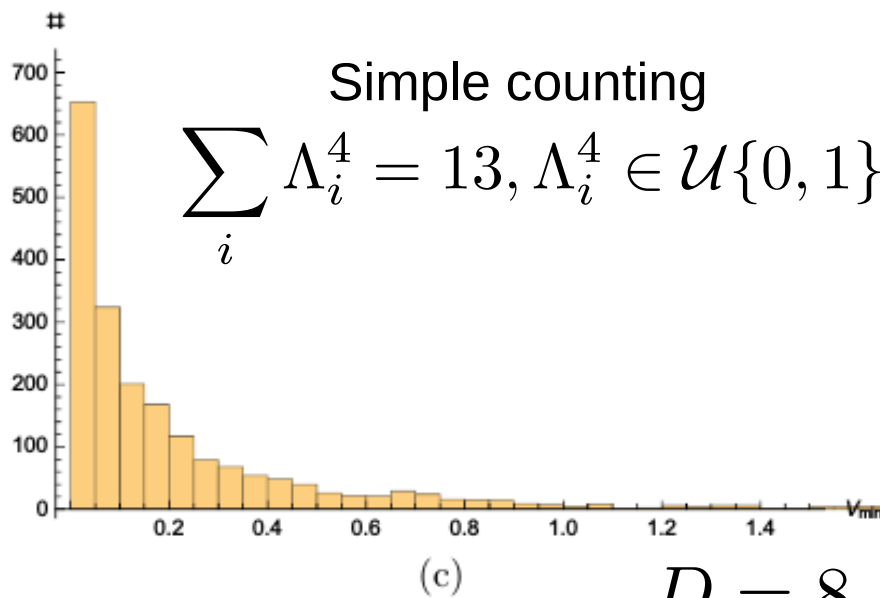
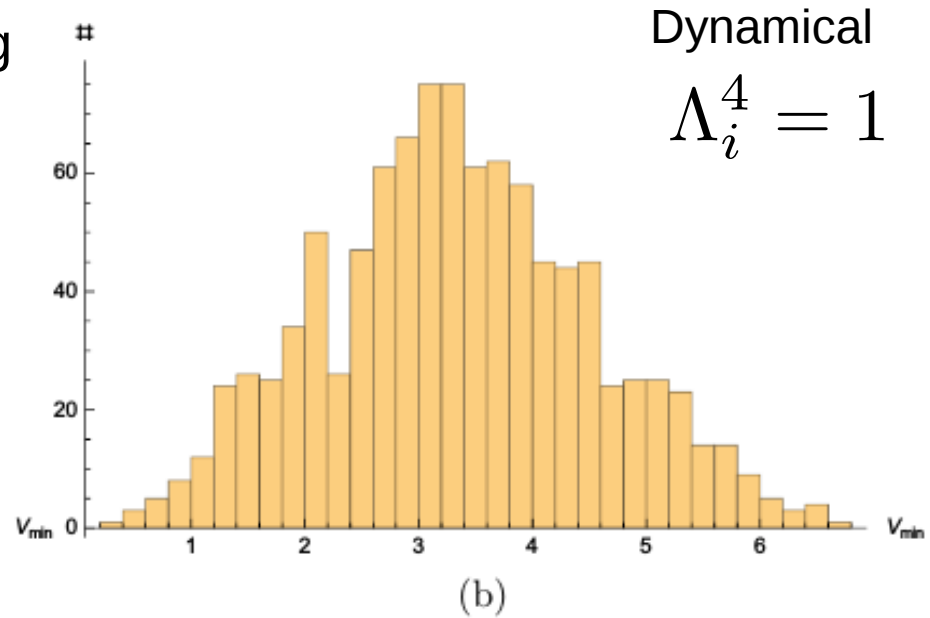
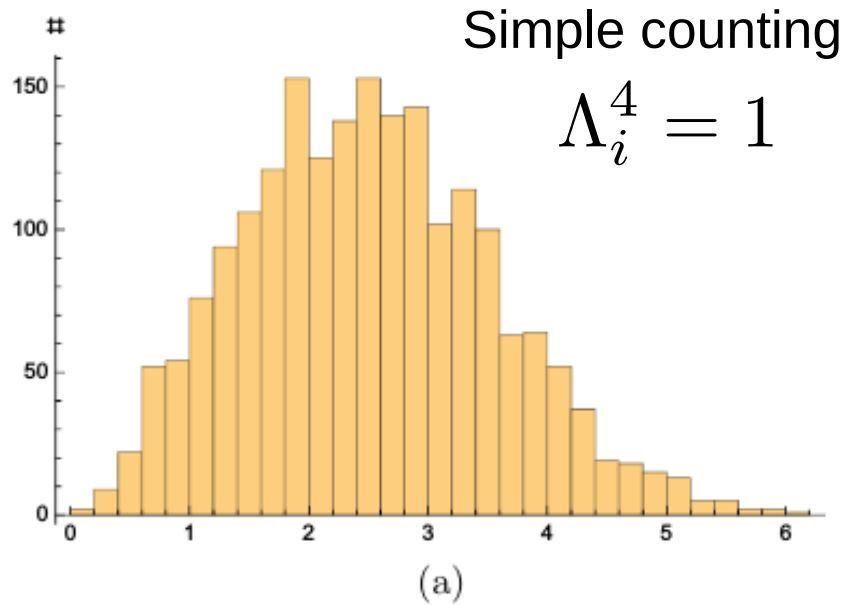
$$\Lambda_i^4 \in \mathcal{U}\{0, 1\}$$

$$n_{ij} \in \mathcal{N}\{0; 2\} (|n_{ij}| < 3)$$

$$V = \sum_{i=1}^{N_{source}} \Lambda_i^4 \left( 1 - \cos \left( \sum_{j=1}^{N_{axion}} n_{ij} \frac{\phi_j}{f_j} + \theta_i \right) \right) + C$$


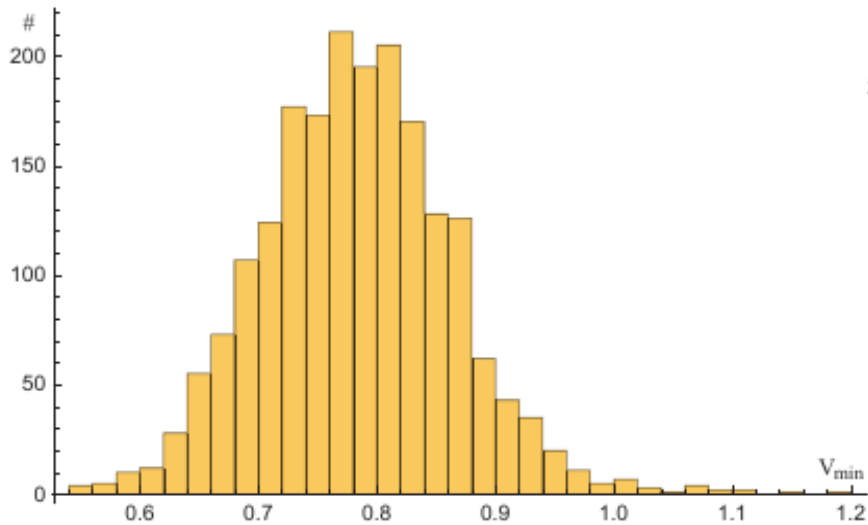
J.E. Kim, H.P. Nilles, M. Peloso 2004  
M. Kawasaki, K. Nakayama 2013  
T. Higaki, F. Takahashi 2014

# Numerical approach

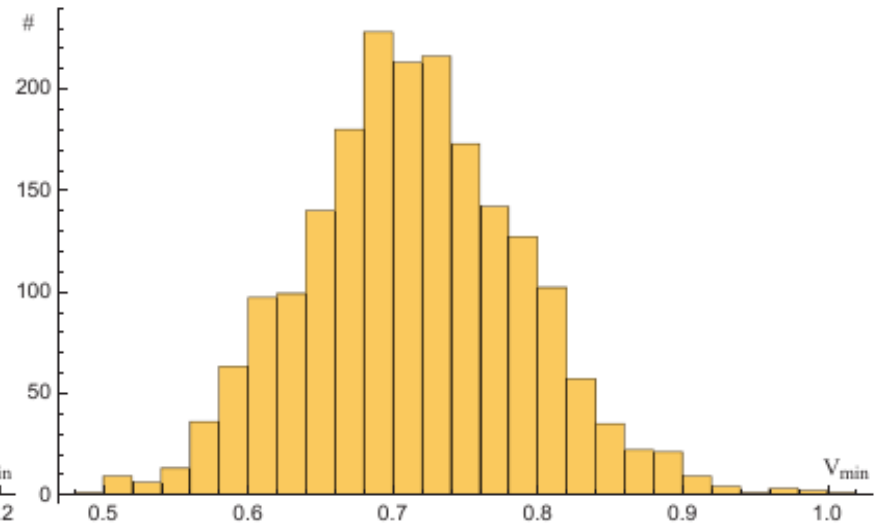


$$D = 8, N_s = 13$$

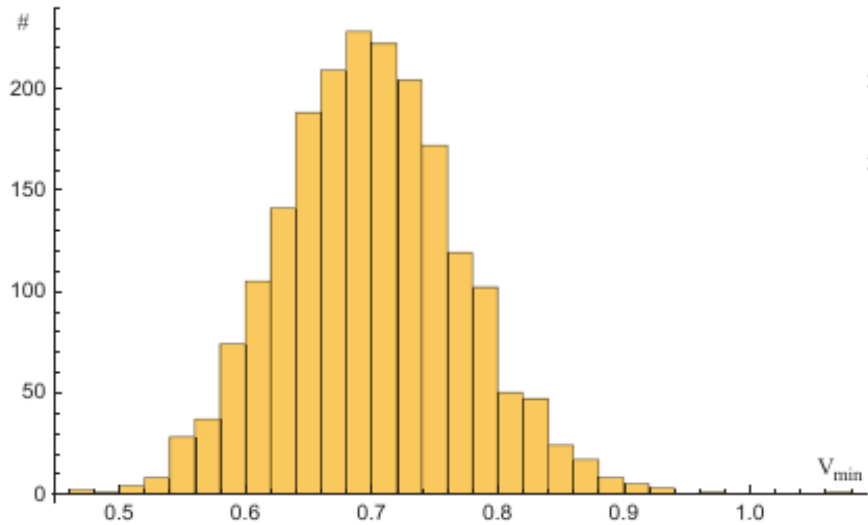
# Numerical approach



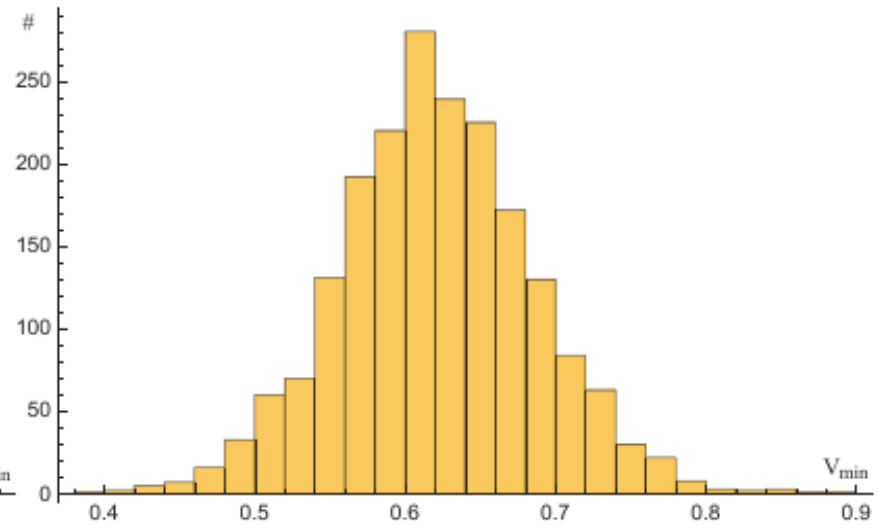
(a) 3D



(b) 4D



(c) 5D



(d) 6D

$$N_s = 125$$

# Analytical approach – Methods

R.Easter, L. McAllister 2005

- Number of minima to

number of critical points ratio:

-Random Matrix Theory (RMT)

$$P_{min} = \frac{\#Minima}{\#Critical\ points}$$

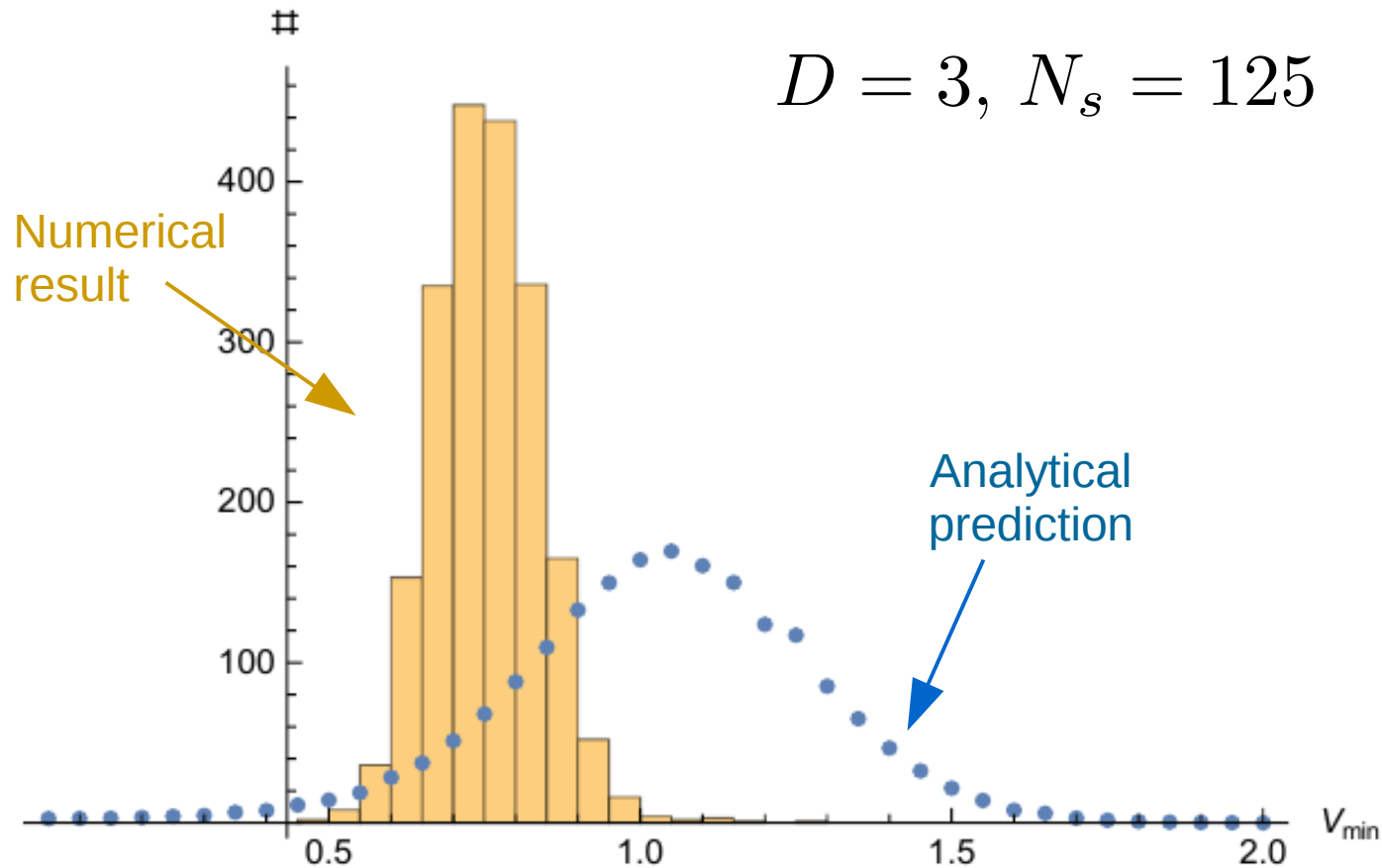
- Mean distance to the next critical point  $\Delta V$

-Ansatz (numerically tested)



Expectation value for the peaks

# Analytical approach



- However, no knowledge about dynamics!



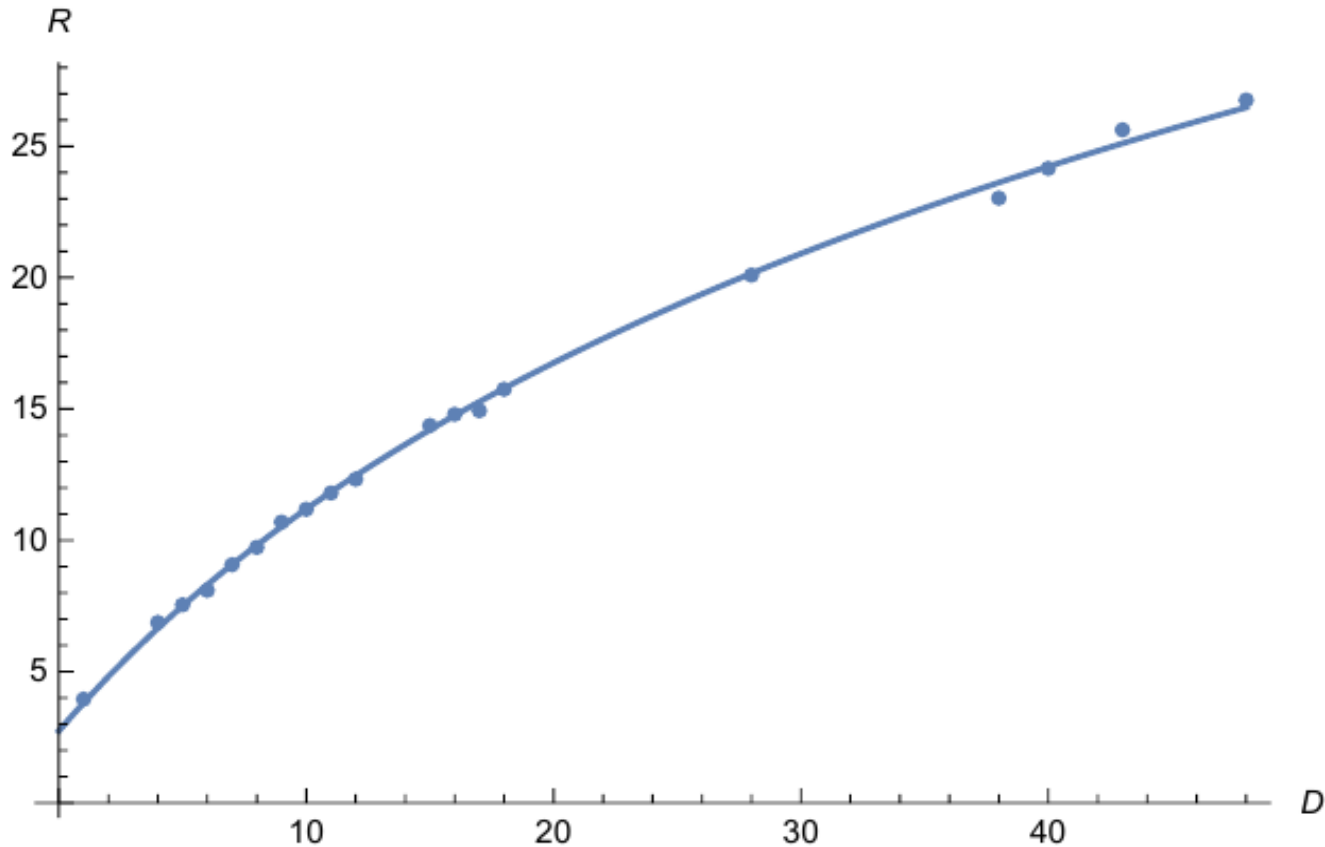
# Empirical approach

- Abandon RMT

$$P_{min} \neq \frac{\# \text{Minima}}{\# \text{Critical points}} \quad \text{We define:} \quad R(D) = \frac{dV}{\Delta V}$$

- Determine the minimum to critical point ratio  $R(D)$  empirically.
- Use analytical value for  $\Delta V$ .
- Combine  $R(D)$  and  $\Delta V$  to obtain the final resting place.

# Empirical approach – $R(D)$

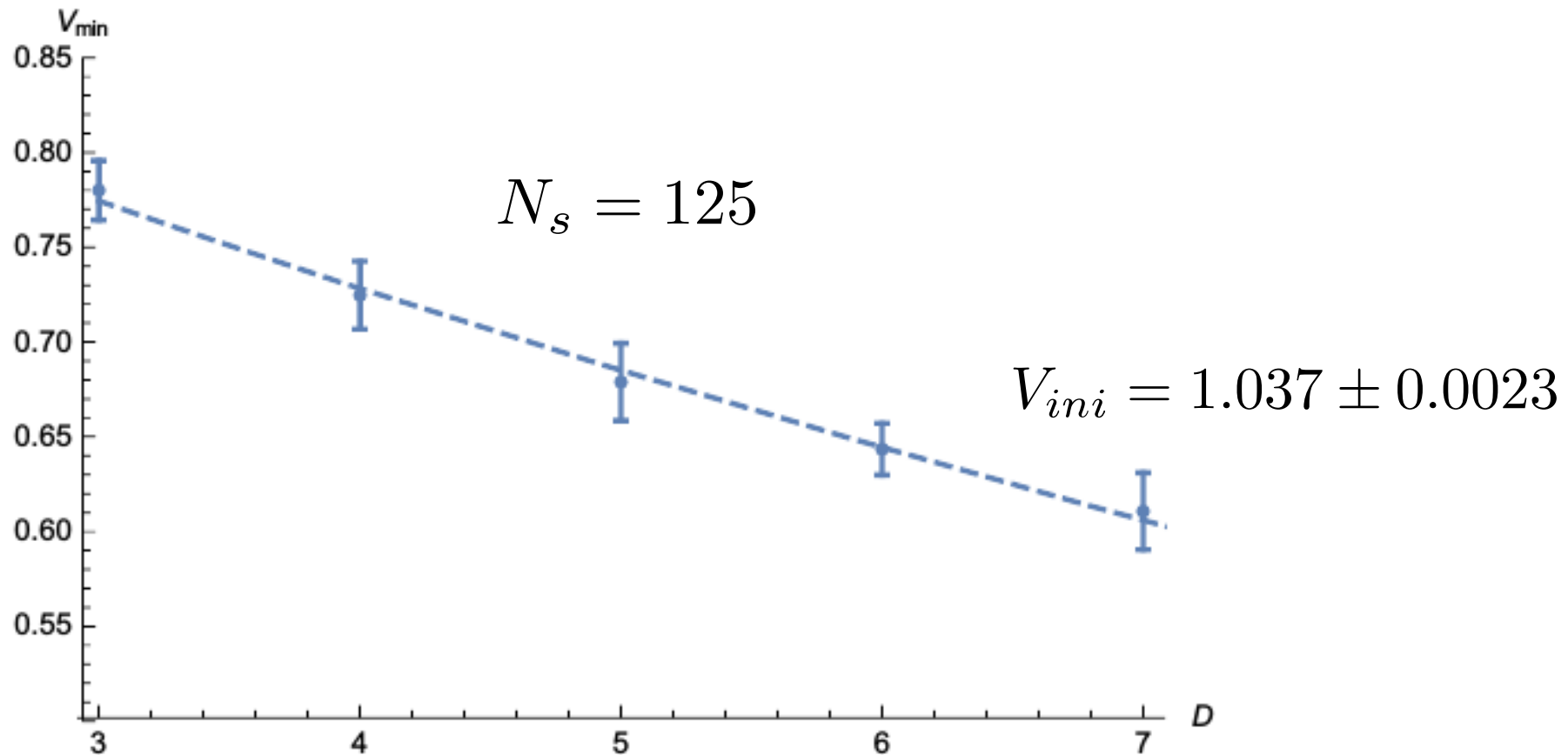


$R(D)$  is computed numerically for selected  $D$  and  $N_s = 125$ .  
 $R(D)$  is not a function of  $N_s$

**Best fit:**  $R(D) = 16.38 \ln(15 + D) - 41.56$

# Final resting place

$$V_{min}(D, N_s) = V_{ini} - dV(D, N_s) = V_{ini} - R(D) \cdot \Delta V$$



(a)  $\bar{V}_{min}$

Comparison of  $V_{min}$  as a function of  $D$  with the numerical results.

# Conclusion

- We successfully predict the peaks.
- Need include dynamics.
- RMT can't explain the logarithms dependency.
- Quantum stability? [A. Masoumi, A. Vilenkin 2016](#)

# Next step

- Develop computational efficient techniques to study these landscapes

[M.C.D. Marsh, L. McAllister, E. Pajer, T. Wrase 2013](#)  
[T. Battefeld, C. Modi 2014](#)

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