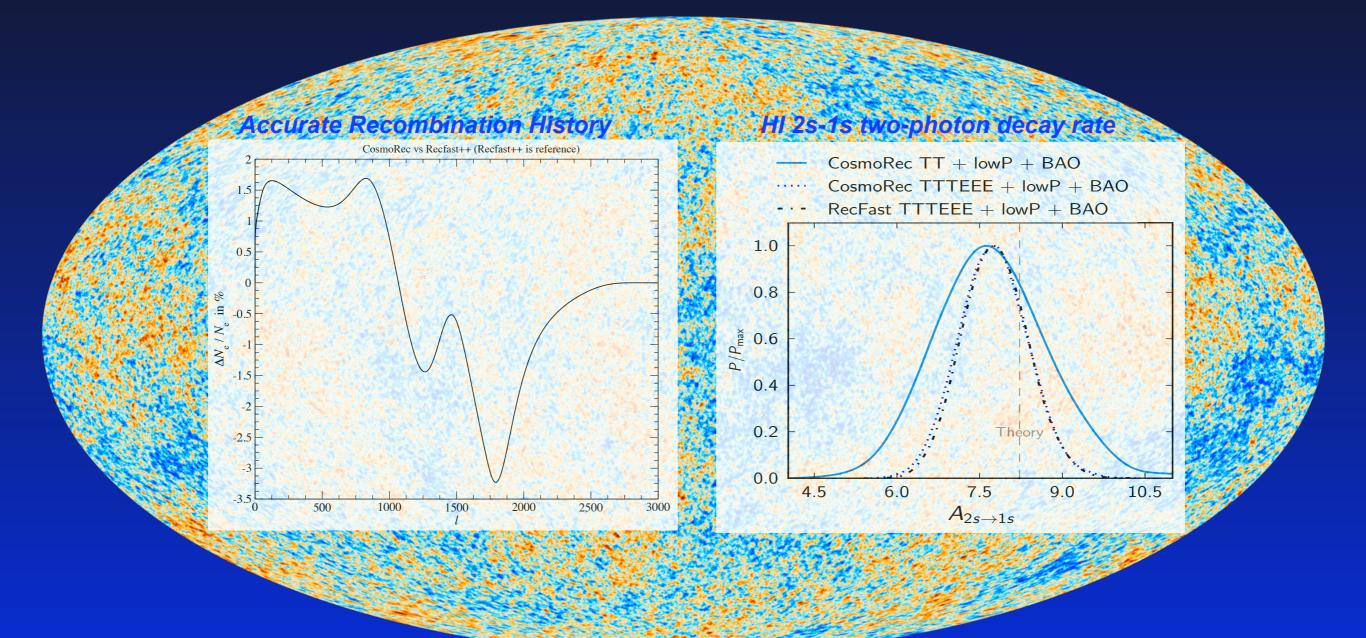
Understanding the Cosmological Recombination Problem to ~0.1% Precision



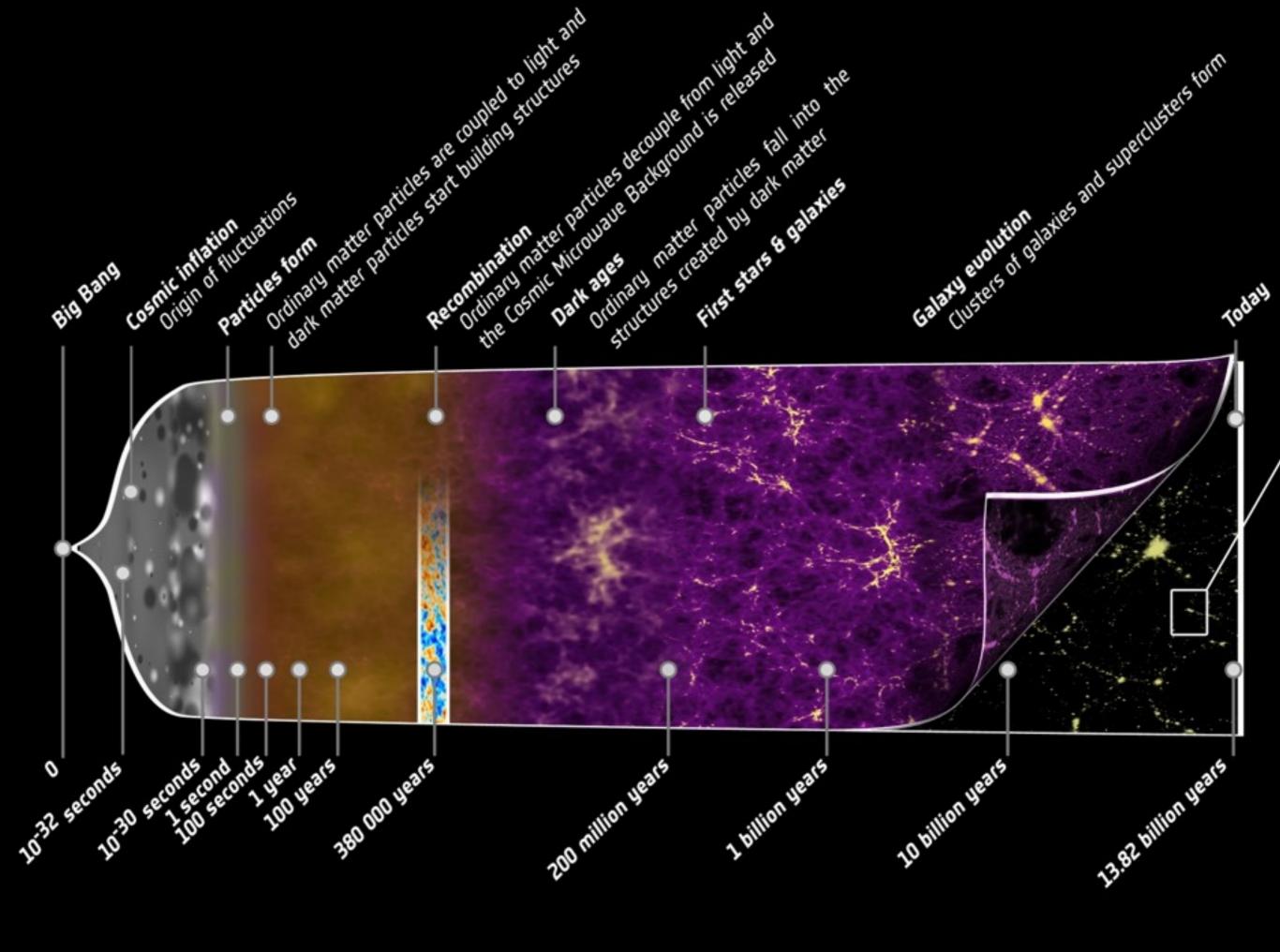


The University of Manchester

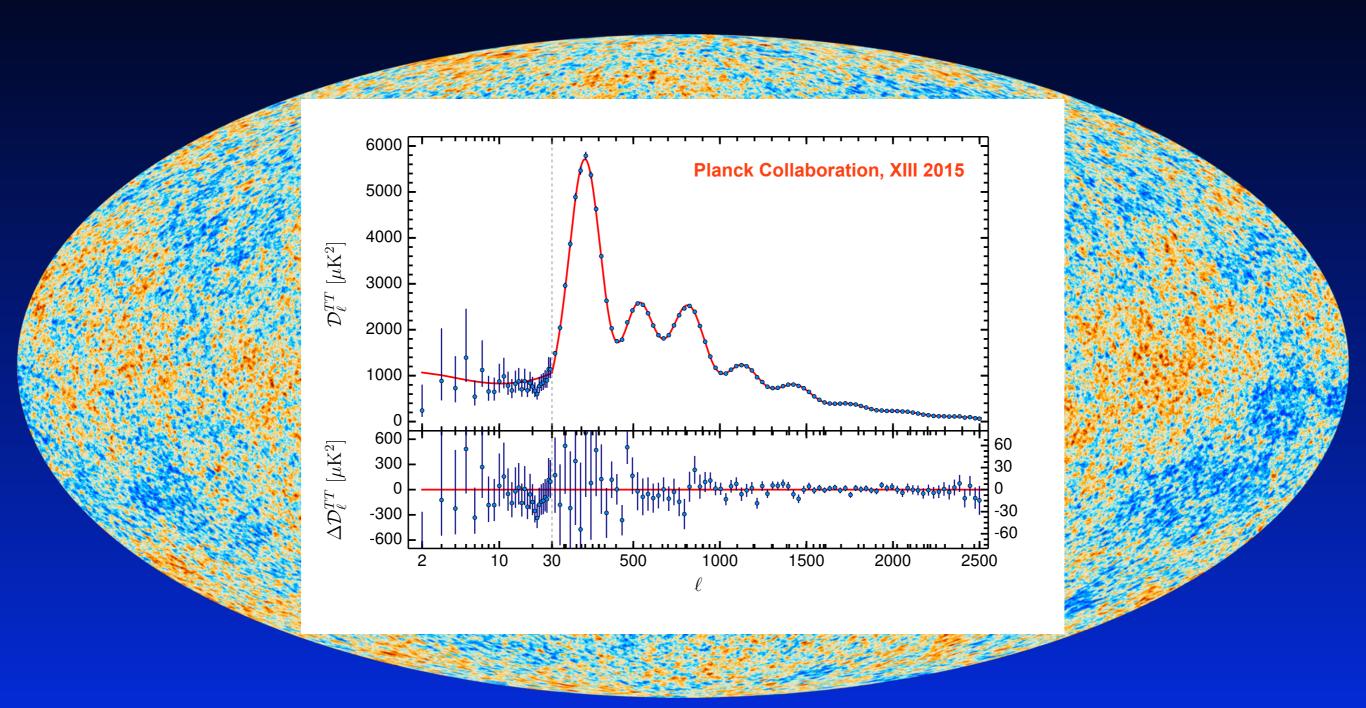
Jens Chluba

The Reionization History of the Universe Bielefeld, Germany, March 8th - 9th, 2018



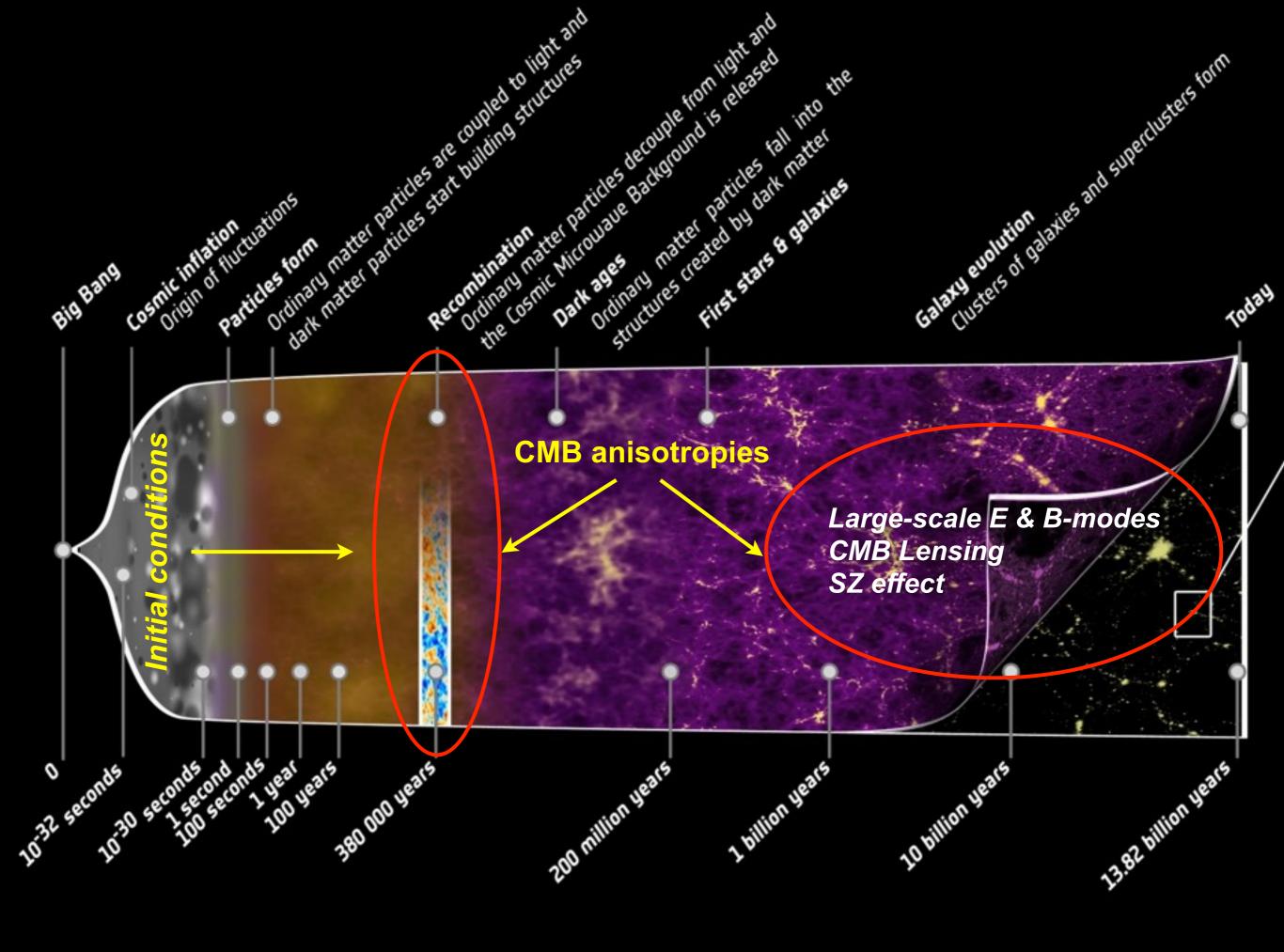


Cosmic Microwave Background Anisotropies

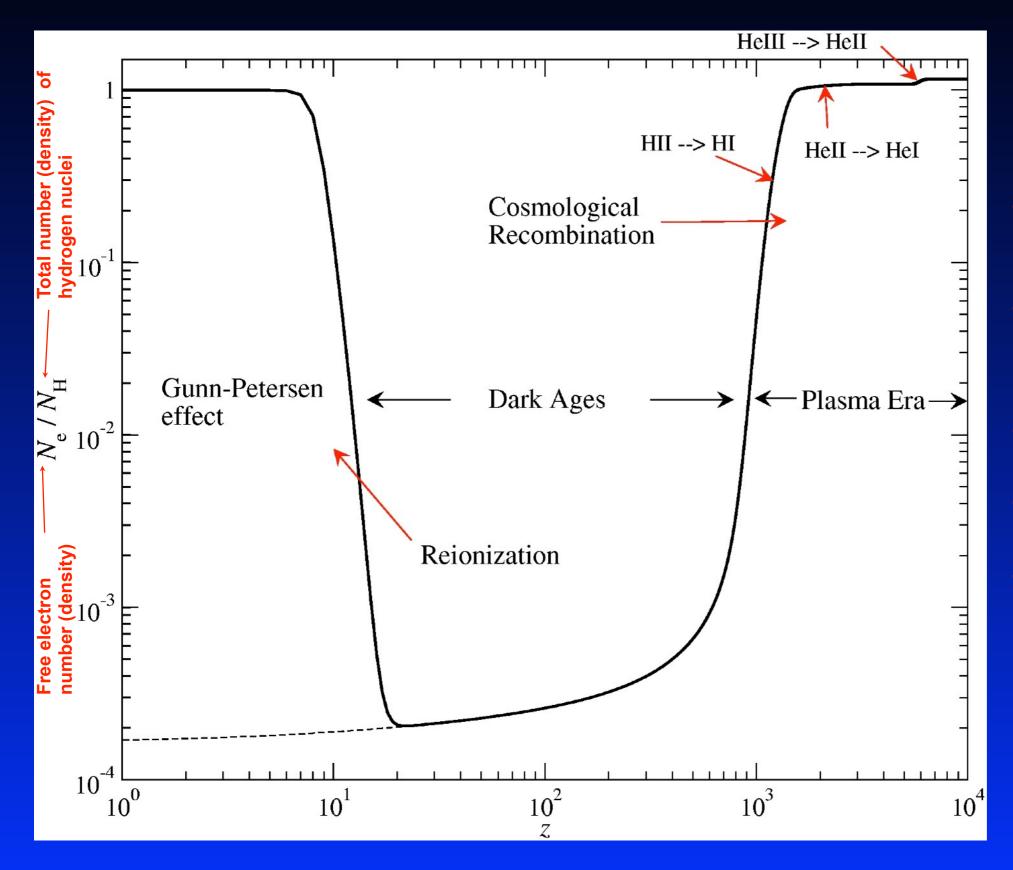


Planck all sky map

- CMB has a blackbody spectrum in every direction
- tiny variations of the CMB temperature $\Delta T/T \sim 10^{-5}$

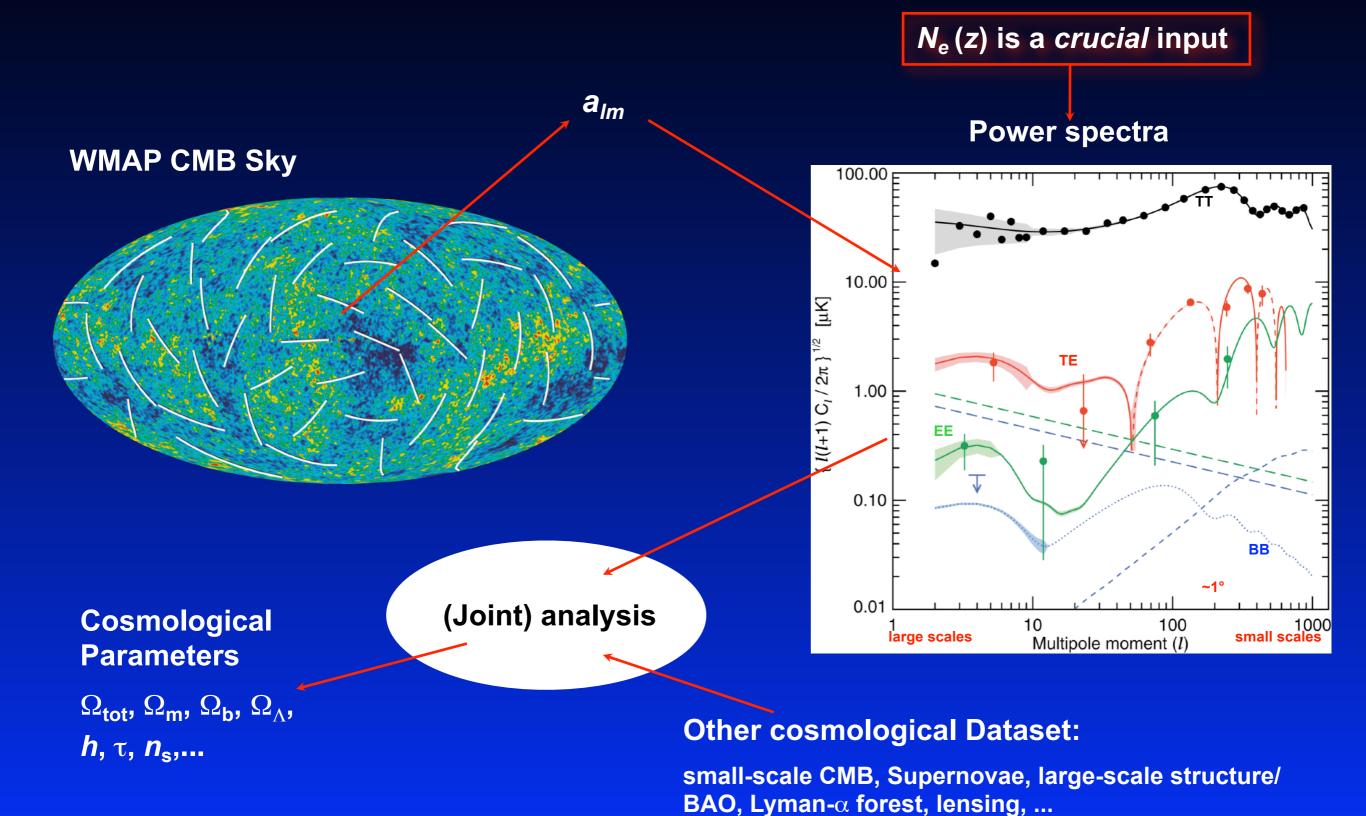


Sketch of the Cosmic Ionization History

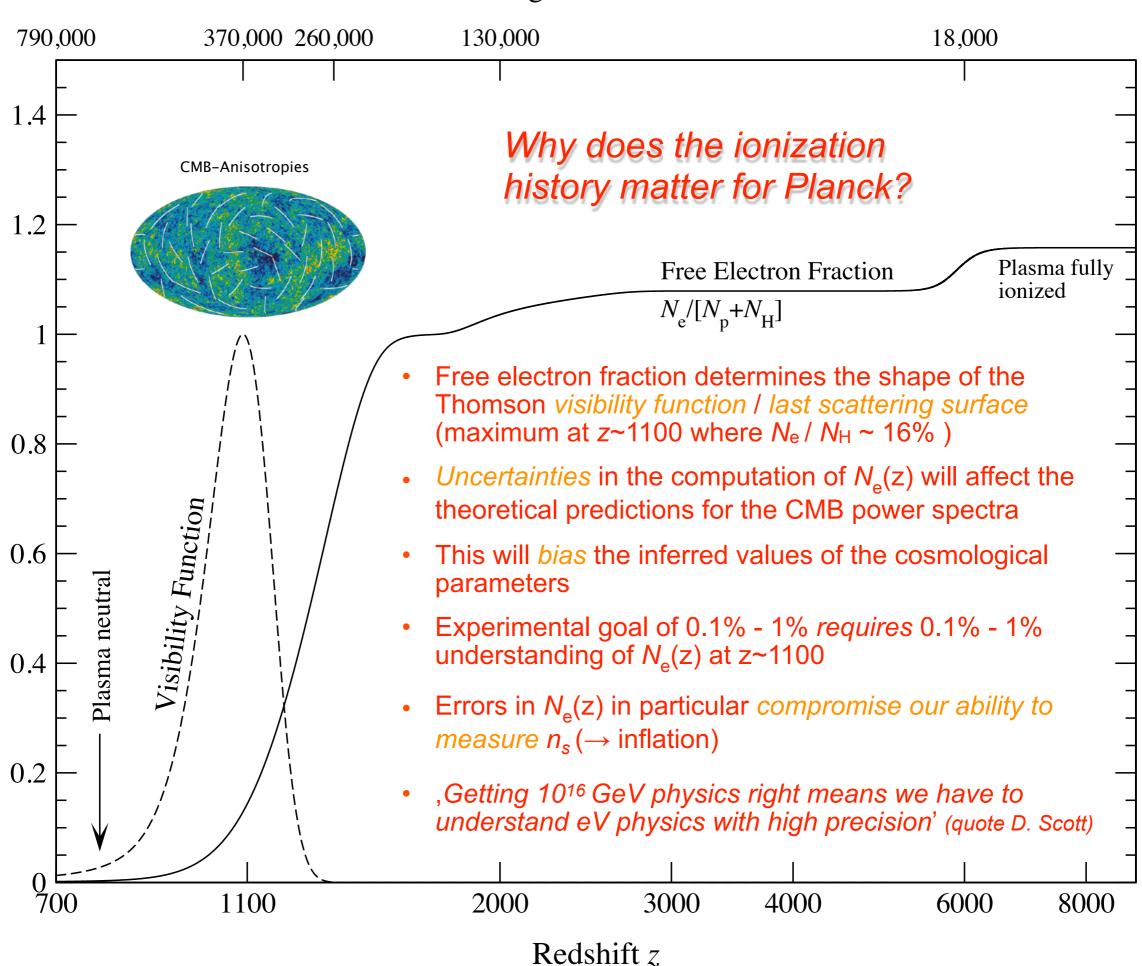


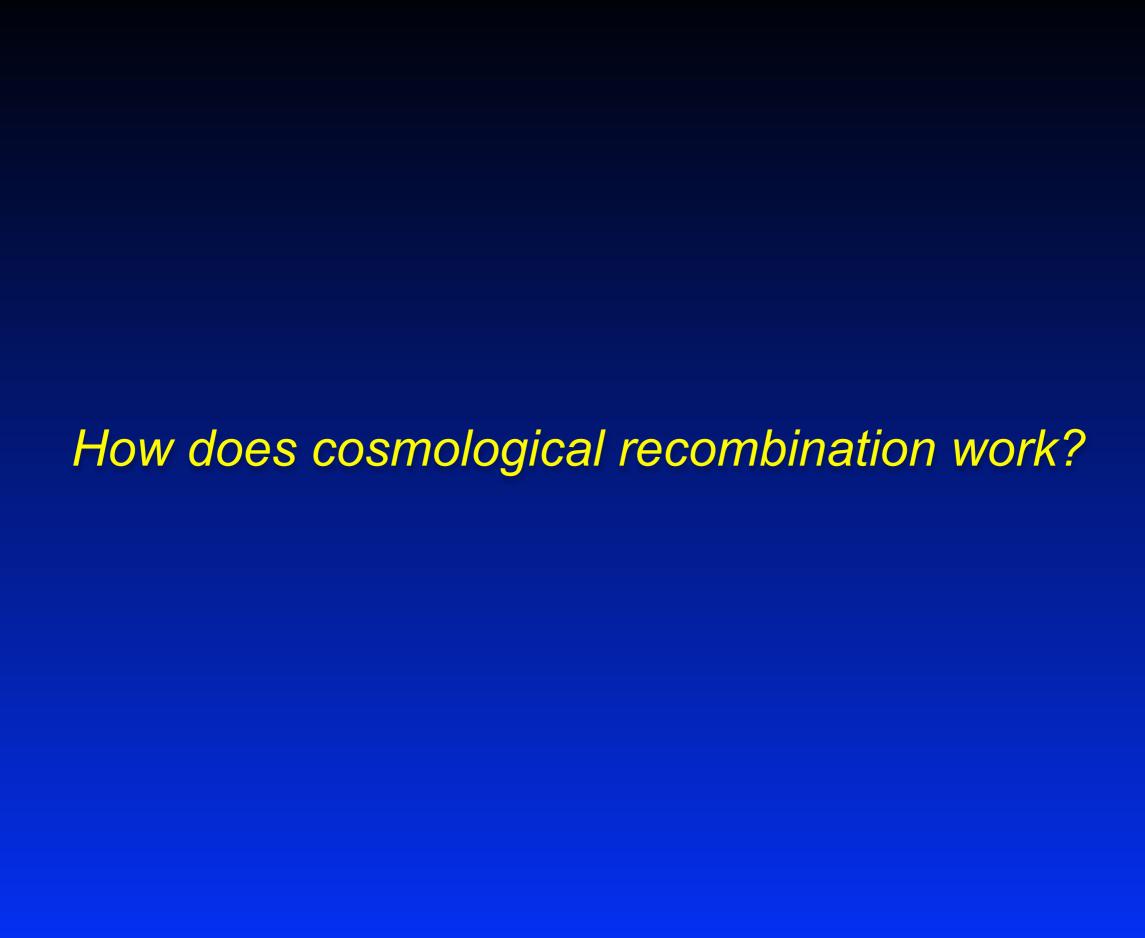
- at redshifts higher than ~10⁴ Universe → fully ionized
- z ≥ 10⁴ → free electron fraction N_e/N_H ~ 1.16
 (Helium has 2 electrons and abundance ~ 8%)
- HeIII → HeII recombination at z~6000
- HeII → HeI recombination at z~2000
- HII → HI recombination at z~1000

CMB Sky → Cosmology



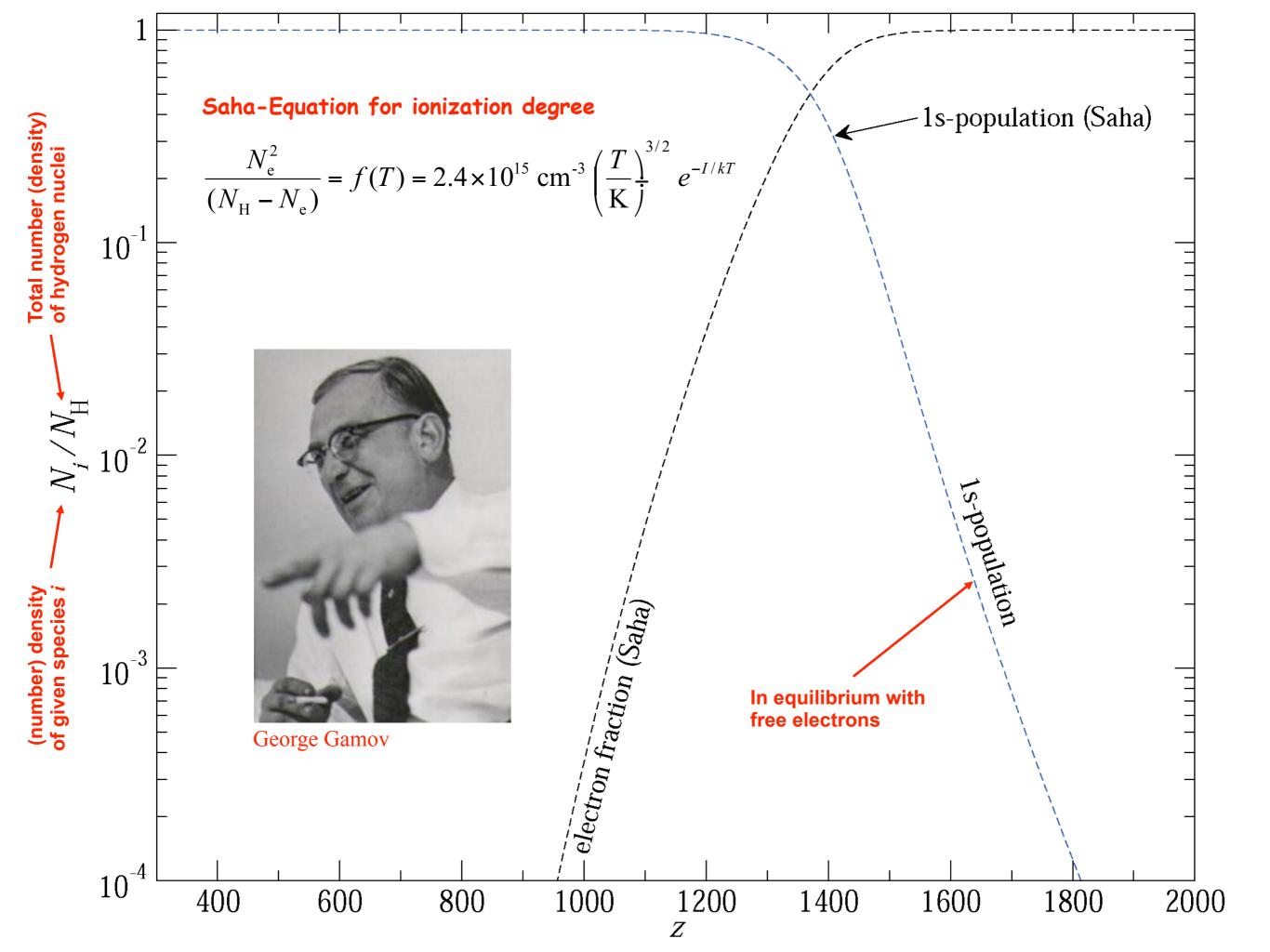
Cosmological Time in Years

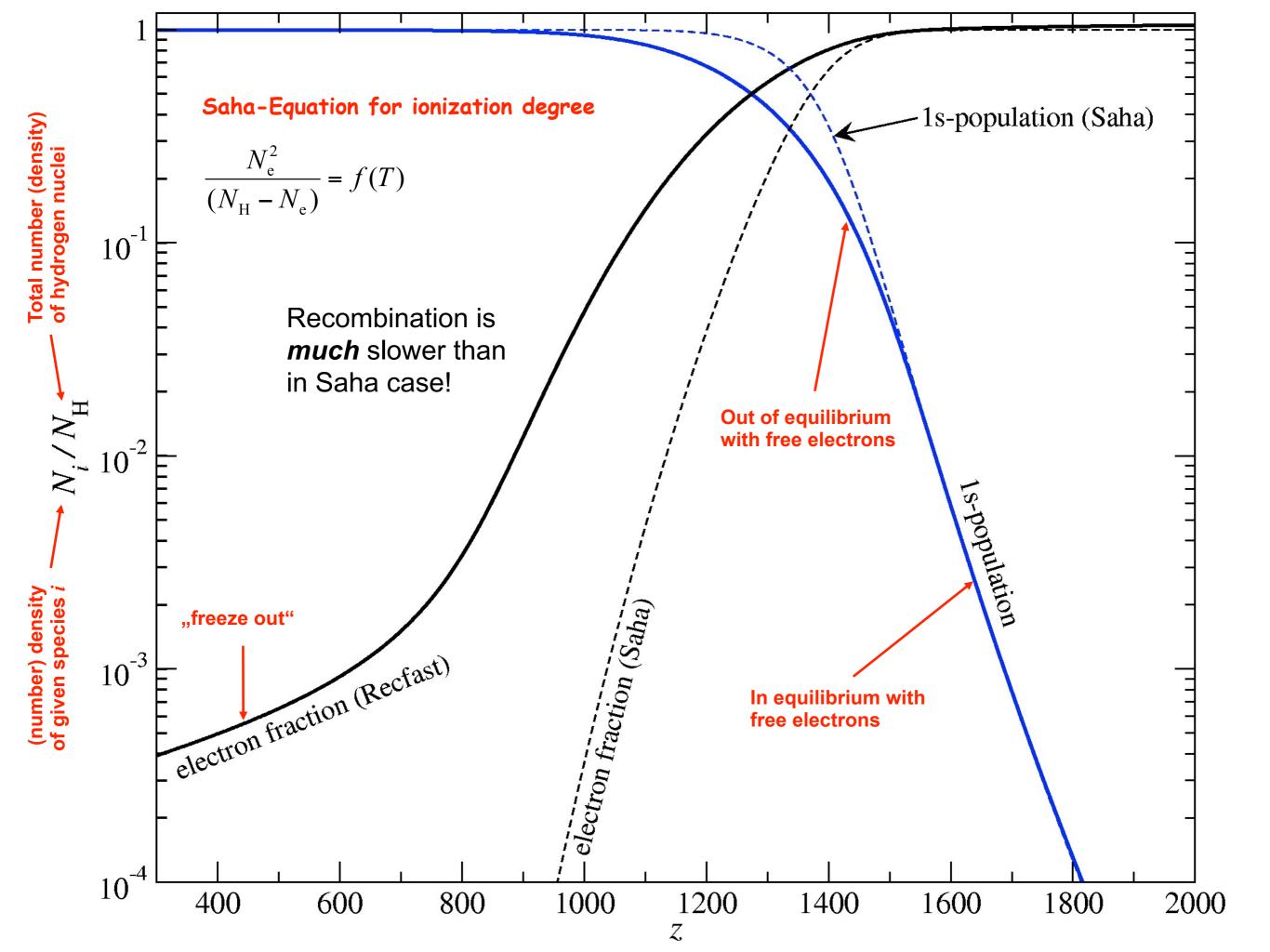




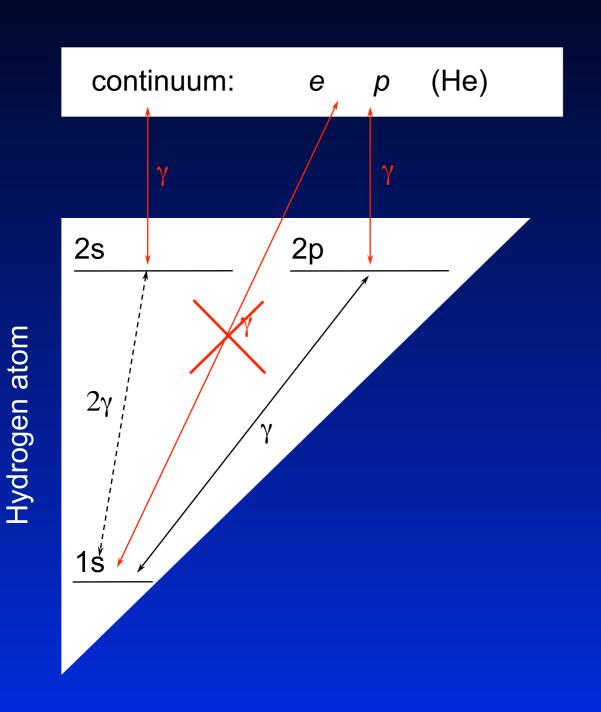
Physical Conditions during Recombination

- Temperature $T_{\gamma} \sim 2.725 (1+z) \text{ K} \sim 3000 \text{ K}$
- Baryon number density N_b ~ 2.5x10⁻⁷cm⁻³ (1+z)³ ~ 330 cm⁻³
- Photon number density $N_{\gamma} \sim 410 \text{ cm}^{-3} (1+z)^3 \sim 2 \times 10^9 N_{b}$ \Rightarrow photons in very distant Wien tail of blackbody spectrum can keep hydrogen ionized until $hv_{\alpha} \sim 40 \ kT_{\gamma} \Leftrightarrow T_{\gamma} \sim 0.26 \text{ eV}$
- Collisional processes negligible (completely different in stars!!!)
- Rates dominated by radiative processes
 (e.g. stimulated emission & stimulated recombination)
- Compton interaction couples electrons very tightly to photons until $z \sim 200 \Rightarrow T_{\gamma} \sim T_{\rm e} \sim T_{\rm m}$





3-level Hydrogen Atom and Continuum



Routes to the ground state?

- direct recombination to 1s
 - Emission of photon is followed by immediate re-absorption

No

- recombination to 2p followed by Lyman-α emission
 - medium optically thick to Ly- α phot.
 - many resonant scatterings
 - escape very hard (p ~10-9 @ z ~1100)

~ 43%

- recombination to 2s followed by 2s two-photon decay
 - 2s \rightarrow 1s ~108 times slower than Ly- α
 - 2s two-photon decay profile \rightarrow maximum at $v \sim$ 1/2 v_{α}
 - immediate escape

~ 57%

These first computations were completed in 1968!



Moscow

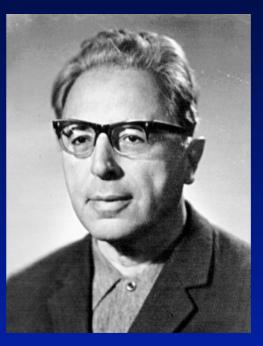


Vladimir Kurt (UV astronomer)

Yakov Zeldovich

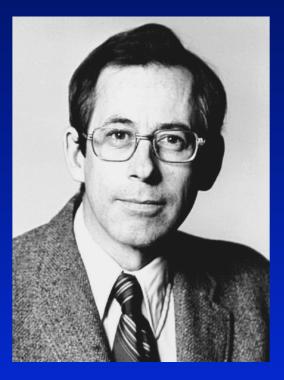


Rashid Sunyaev



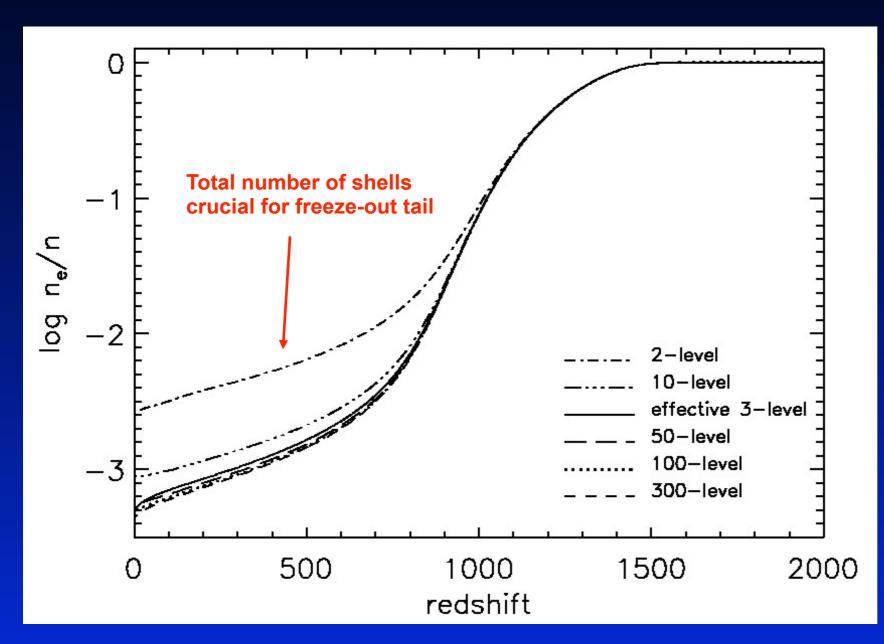
losif Shklovskii

Princeton



Jim Peebles

Multi-level Atom ⇔ Recfast-Code



Output of N_e/N_H

Hydrogen:

- up to 300 levels (shells)
- n ≥ 2 → full SE for *l*-sub-states

Helium:

- Hel 200-levels (z ~ 1400-1500)
- Hell 100-levels (z ~ 6000-6500)
- Helll 1 equation

Low Redshifts:

- H chemistry (only at low z)
- cooling of matter (Bremsstrahlung, collisional cooling, line cooling)

Seager, Sasselov & Scott, 1999, ApJL, 523, L1 Seager, Sasselov & Scott, 2000, ApJS, 128, 407

RECFAST reproduces the result of detailed recombination calculation using fudge-functions

 $\Delta N_{\rm e}$ / $N_{\rm e}$ ~ 1% - 3%

Getting the job done for Planck

Hydrogen recombination

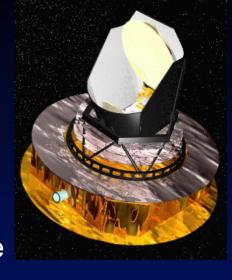
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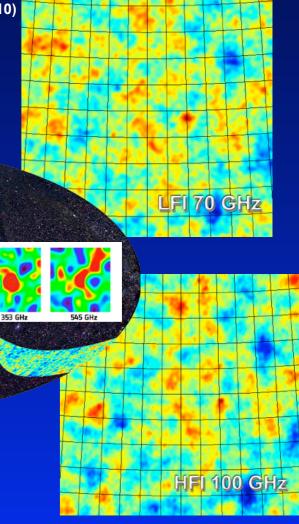


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Helium recombination

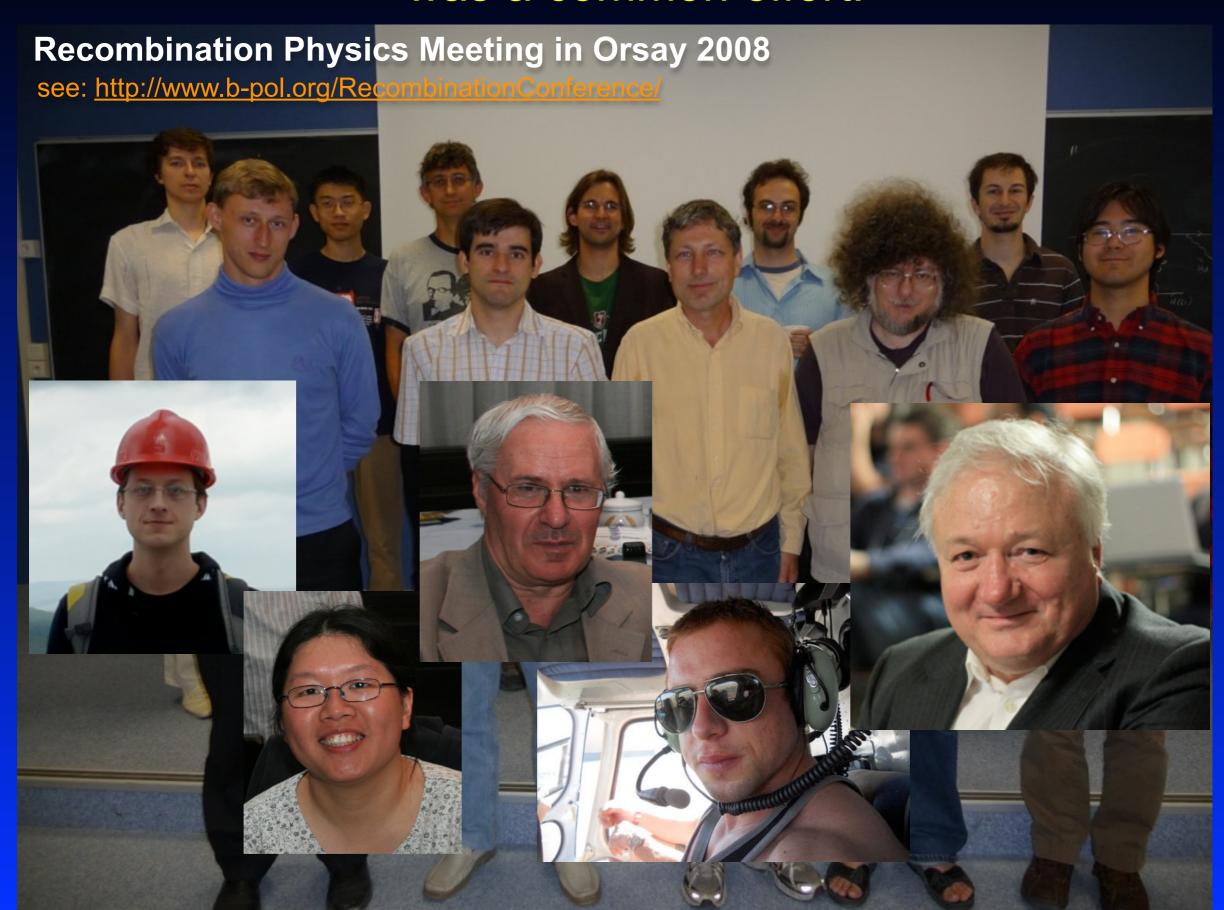
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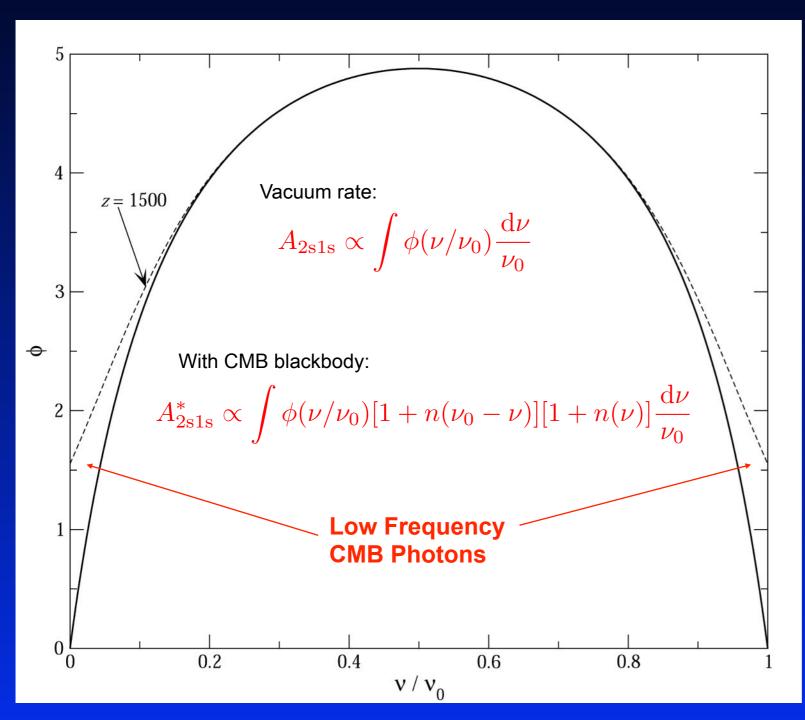


 ΔN_e / N_e ~ 0.1 %

Solving the problem for the *Planck* Collaboration was a common effort!



Stimulated 2s → 1s decay



Transition rate in vacuum

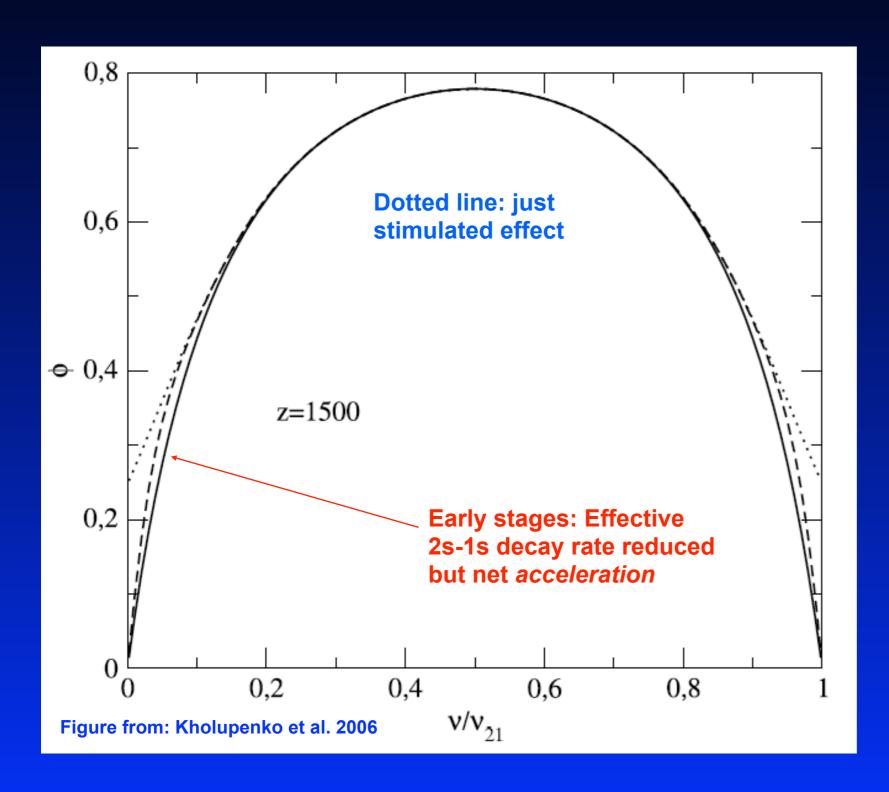
 $\rightarrow A_{2s1s} \sim 8.22 \text{ sec}^{-1}$

CMB ambient photons field

- \rightarrow A_{2s1s} increased by ~1%-2%
- \rightarrow HI recombination faster by $\Delta N_{\rm e}/N_{\rm e} \sim 1.3\%$

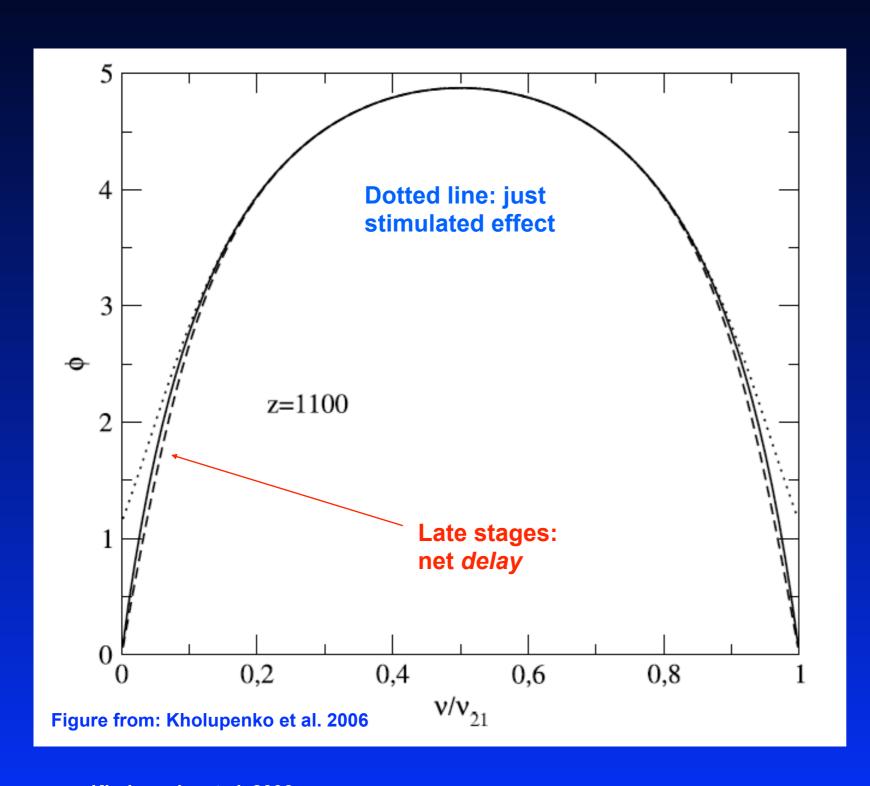
2s-1s emission profile

Feedback of Ly- α on the 1s \rightarrow 2s transition



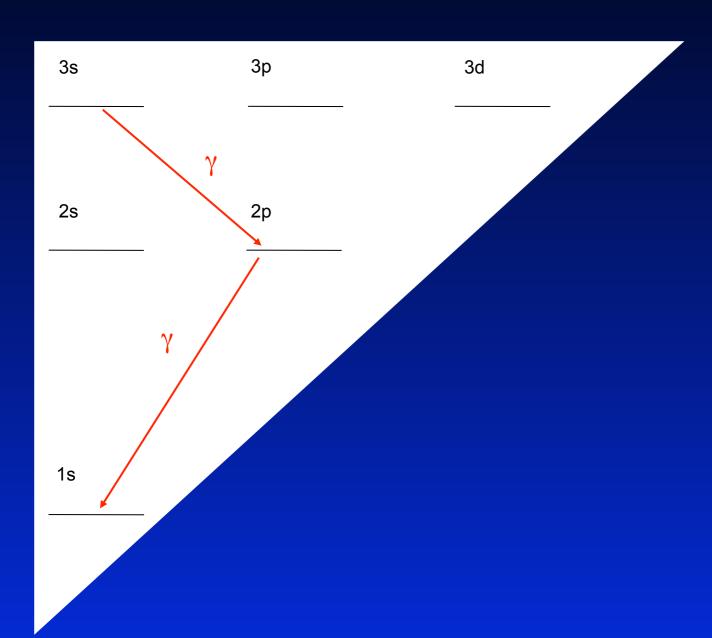
- Some Ly-α photon are reabsorbed in the 1s-2s channel
- delays recombination
- net effect on 2s-1s channel $\Delta N_e/N_e \sim 0.6\%$ around z~1100
- 2s-1s self-feedback $\Delta N_e/N_e \sim -0.08\%$ around $z\sim1100$ (JC & Thomas, 2010)

Feedback of Ly- α on the 1s \rightarrow 2s transition



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Two-photon emission process from upper levels



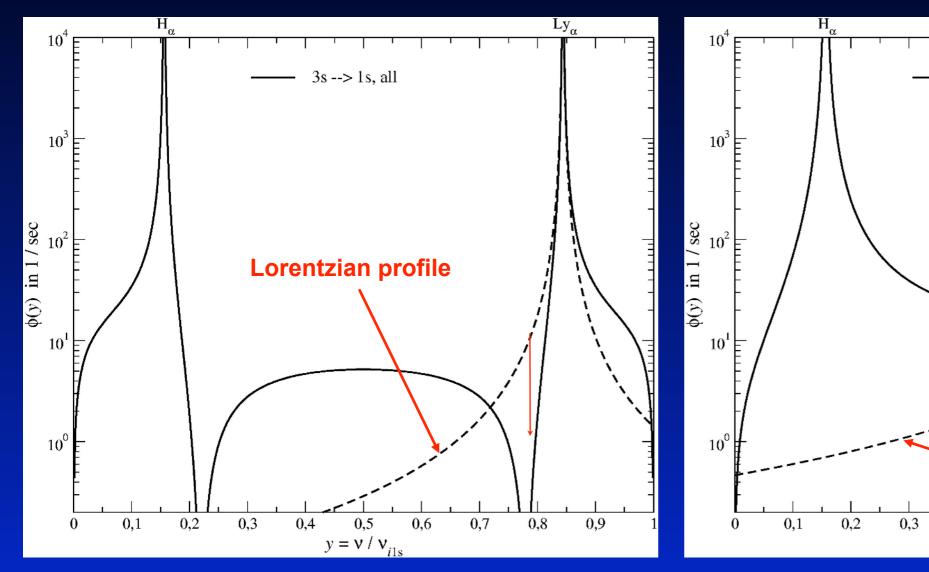
Seaton cascade (1+1 photon)

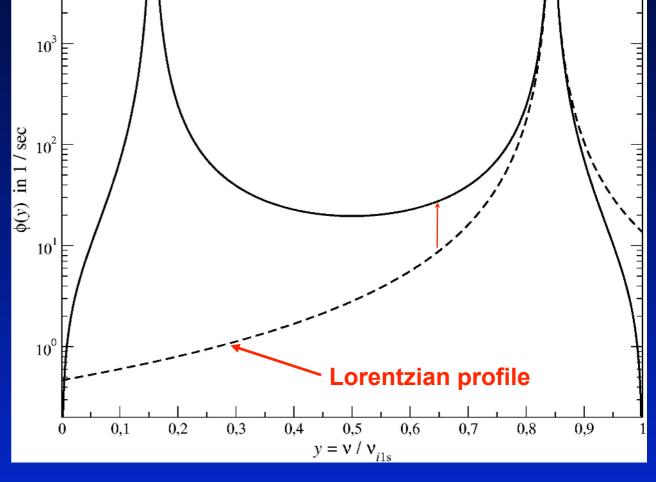
No collisions \rightarrow two photons (mainly H- α and Ly- α) are emitted!

Maria-Göppert-Mayer (1931): description of two-photon emission as single process in Quantum Mechanics

- → Deviations of the *two-photon line profile* from the Lorentzian in the damping wings
- → Changes in the optically thin (below ~500-5000 Doppler width) parts of the line spectra

3s and 3d two-photon decay spectrum





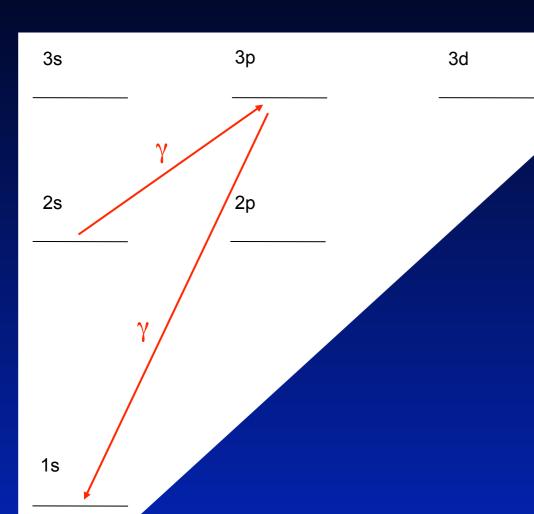
3d --> 1s, all

 Ly_{α}

Direct Escape in optically thin regions:

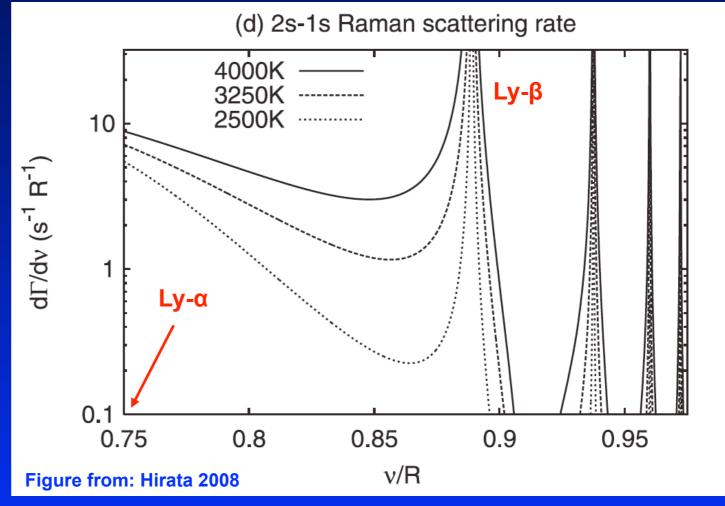
- → HI -recombination is a bit *slower* due to 2γ-transitions from s-states
- HI -recombination is a bit faster due to 2γ-transitions from d-states

2s-1s Raman scattering

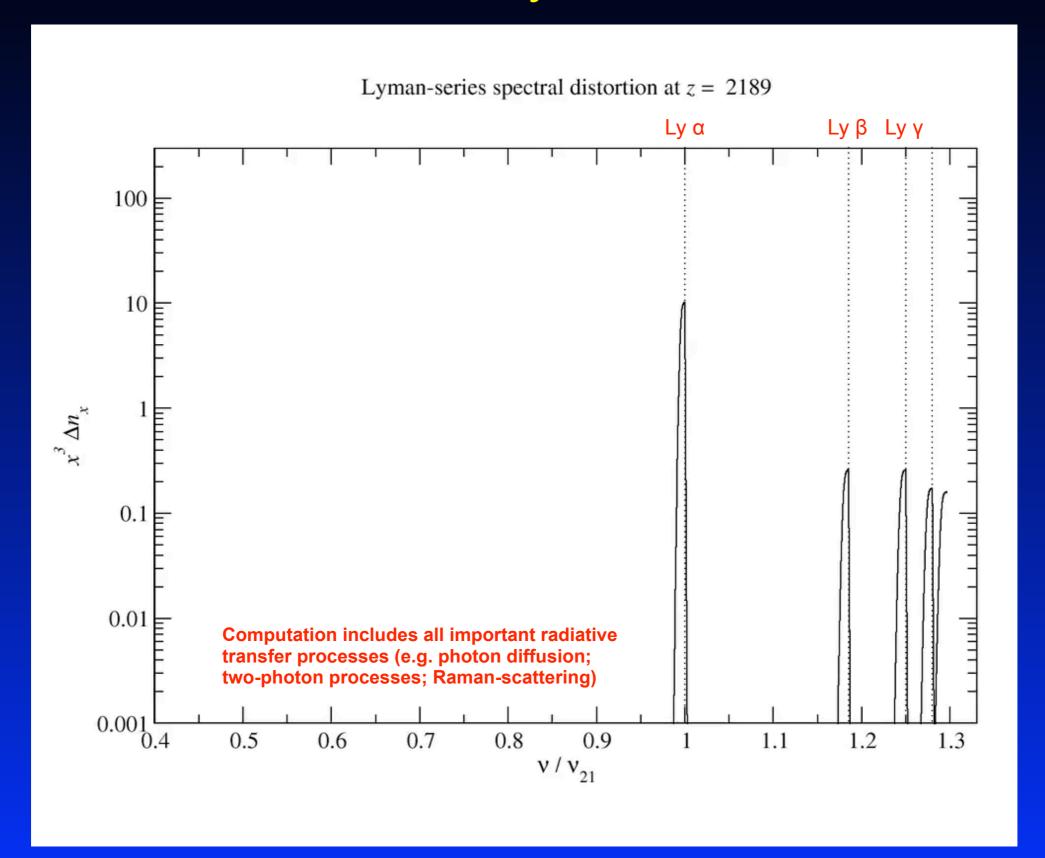


- Enhances blues side of Ly-α line
- associated feedback delays recombination around z~900

- Computation similar to two-photon decay profiles
- collisions weak ⇒ process needs
 to be modeled as single quantum act



Evolution of the HI Lyman-series distortion



Getting the job done for Planck

Hydrogen recombination

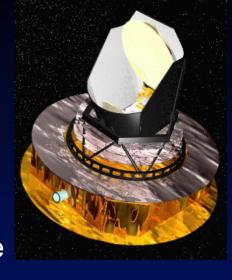
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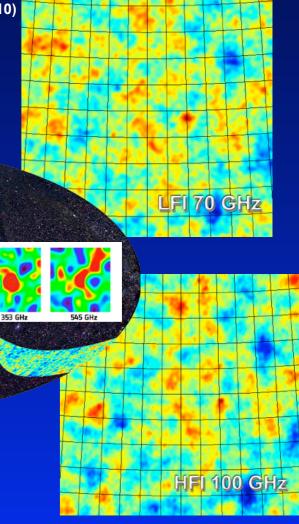


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Helium recombination

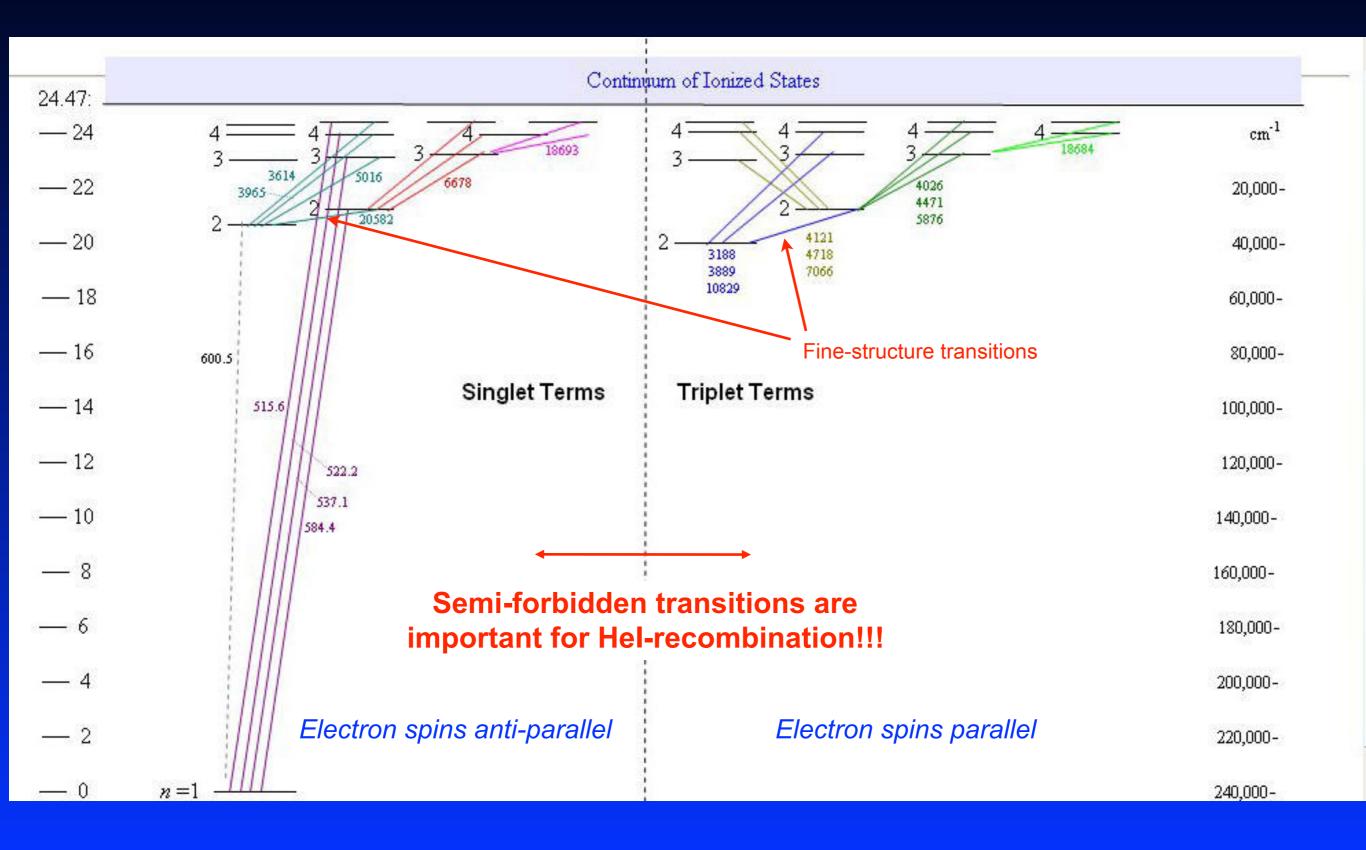
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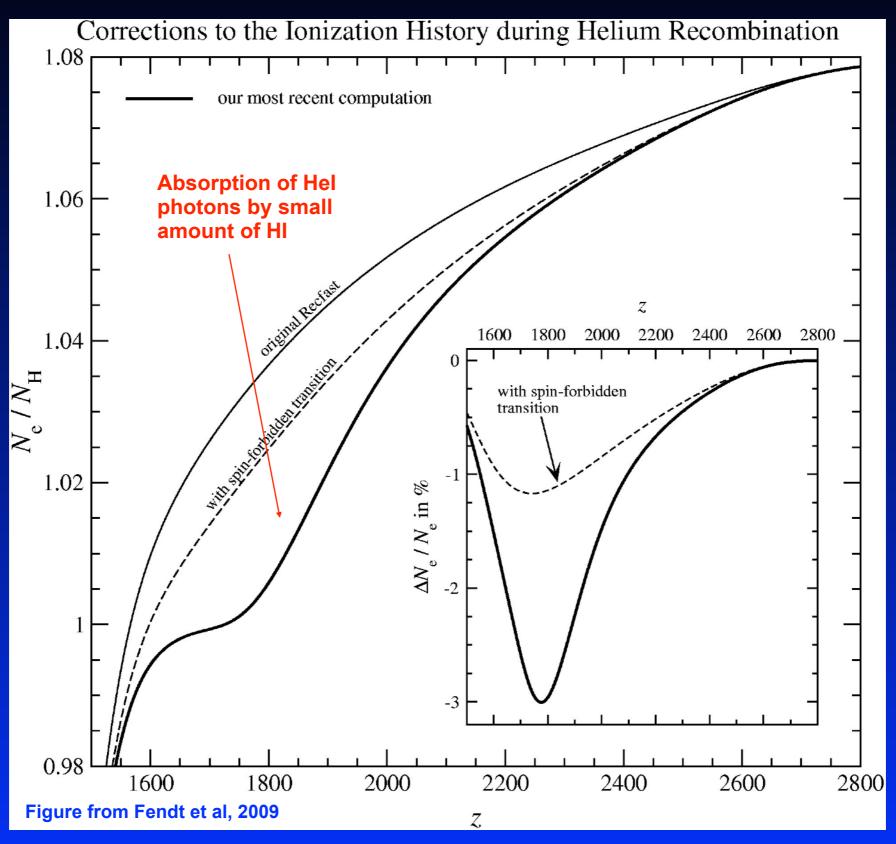


 ΔN_e / N_e ~ 0.1 %

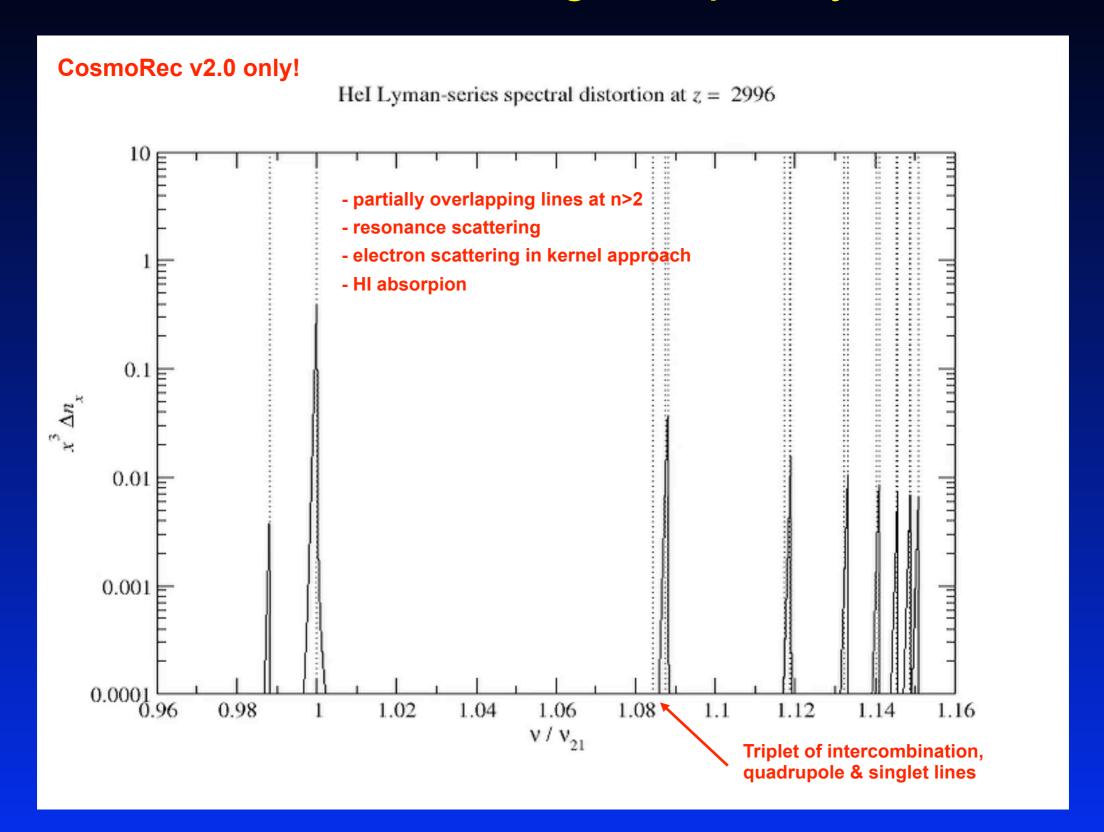
Grotrian diagram for neutral helium



Main corrections during Hel Recombination

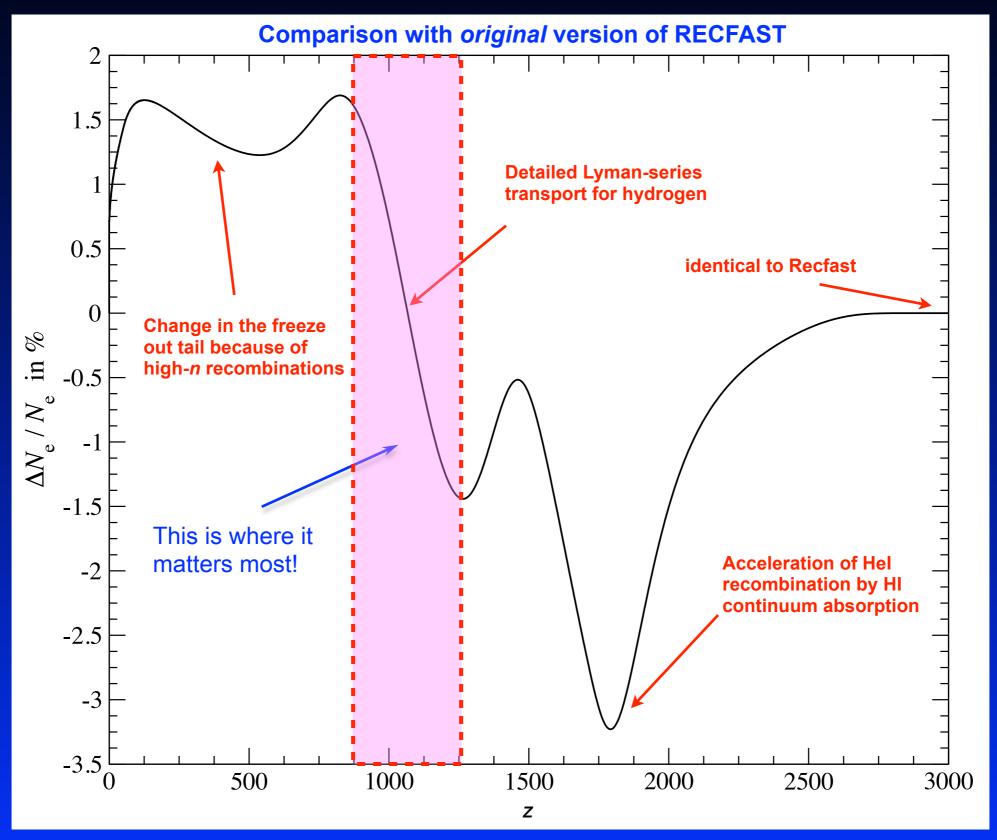


Evolution of the Hel high frequency distortion



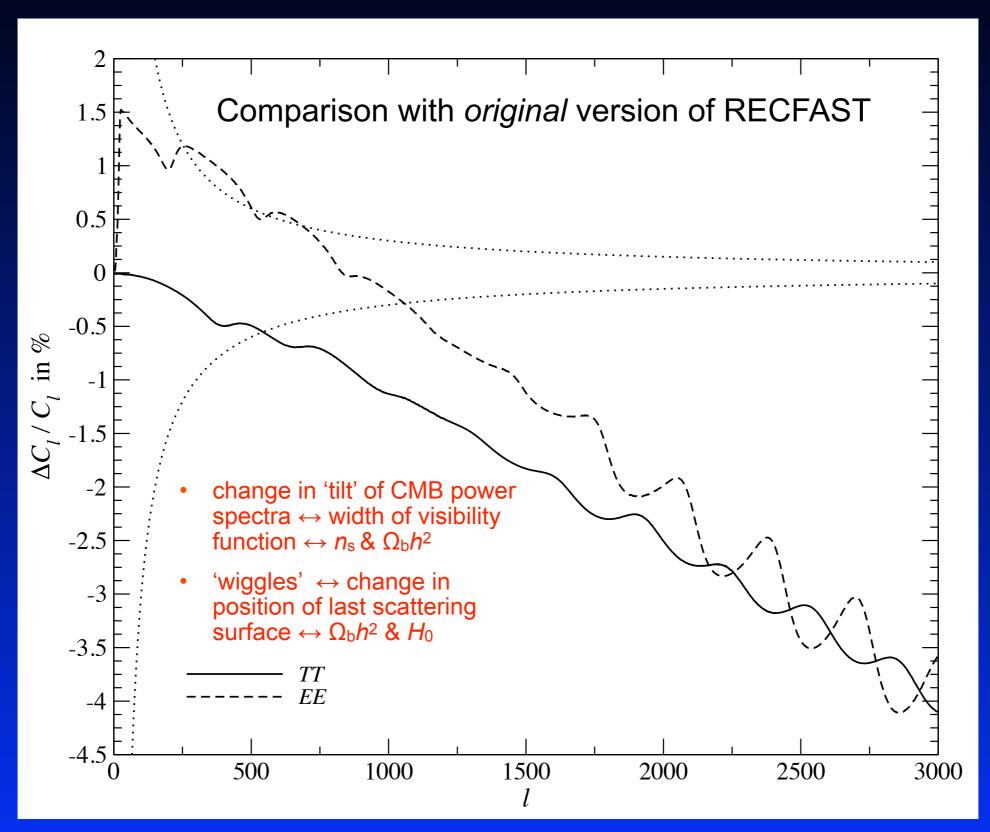


Cumulative Changes to the Ionization History

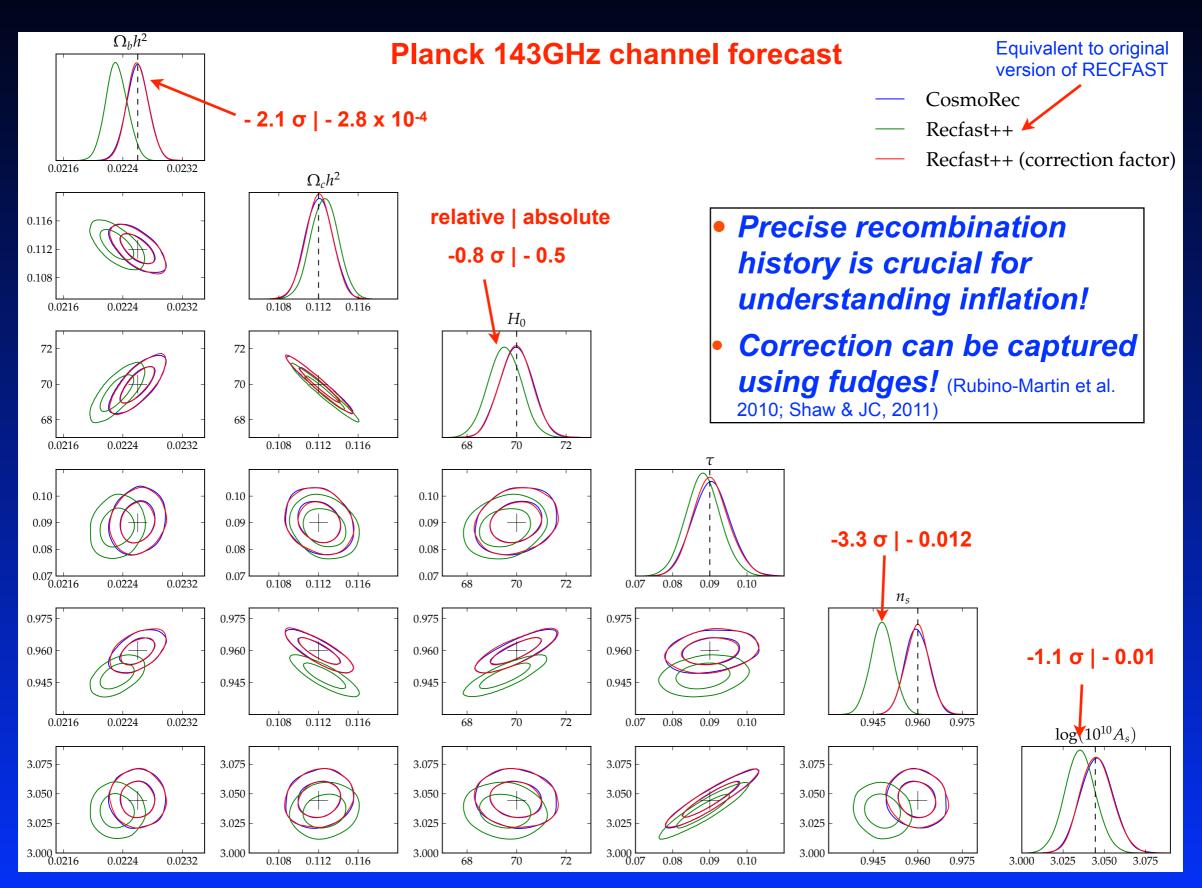




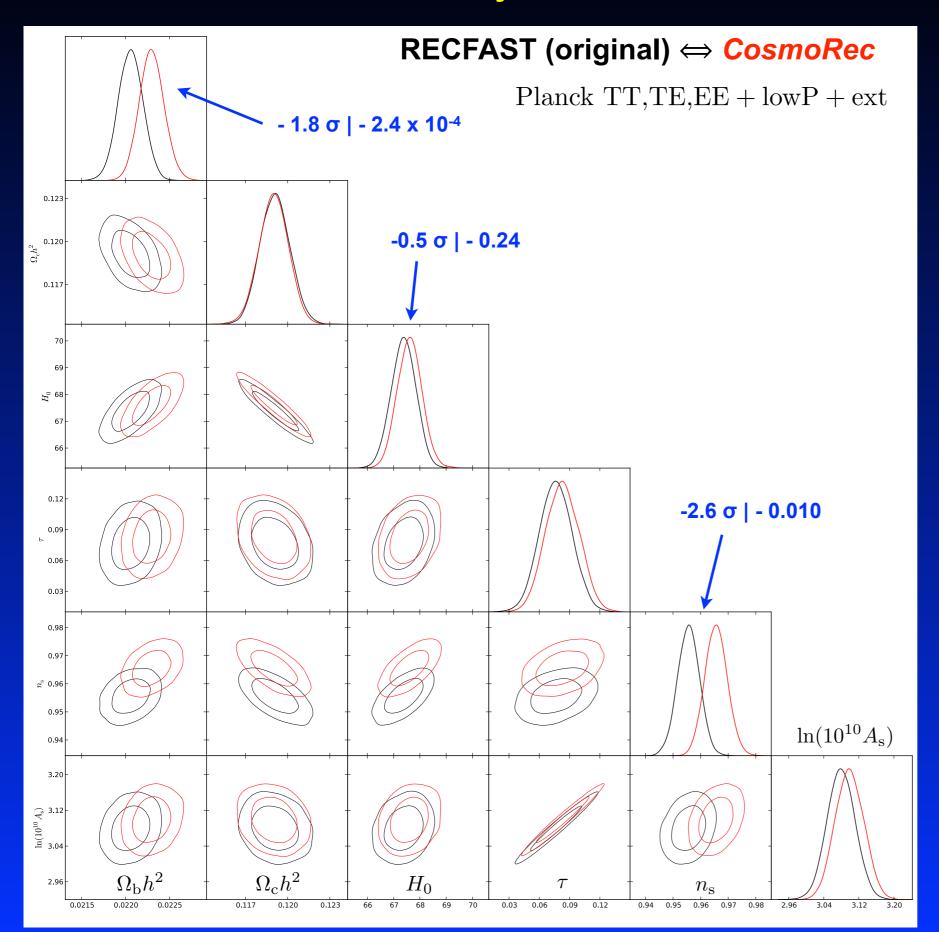
Cumulative Change in the CMB Power Spectra



Importance of recombination for *Planck*



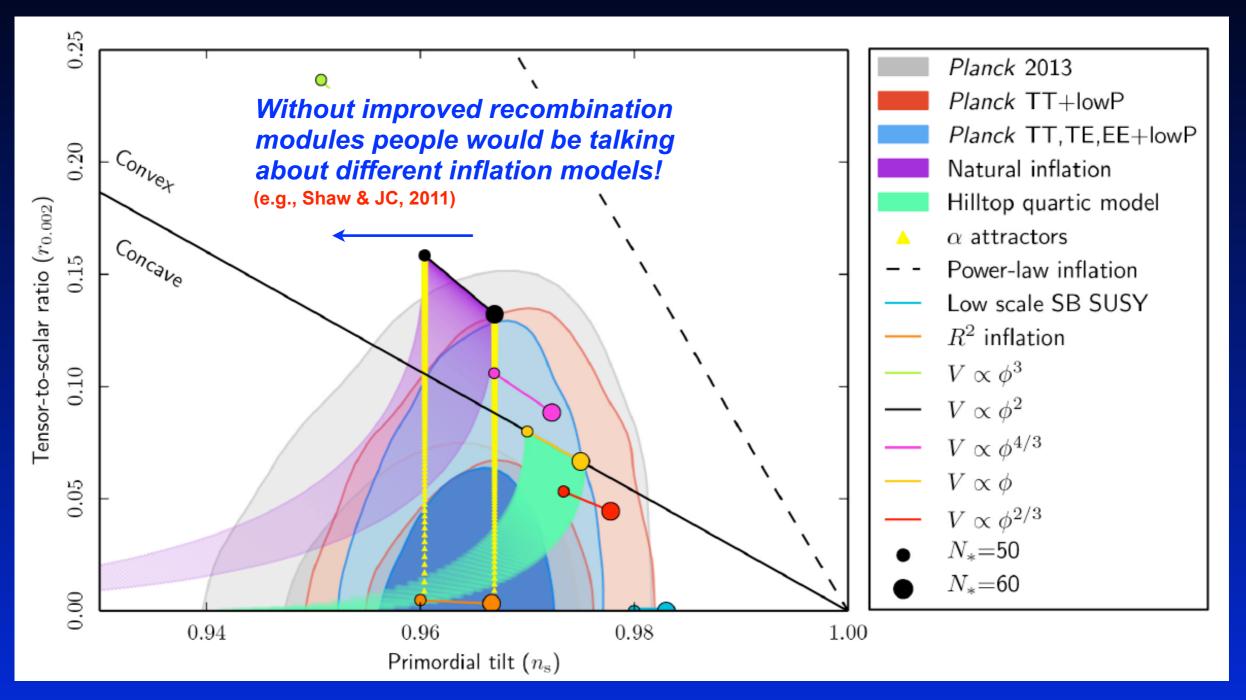
Biases as they would have been for Planck



- Biases a little less significant with real *Planck* data
- absolute biases very similar
- In particular n_s
 would be biased
 significantly

Planck Collaboration, XIII 2015

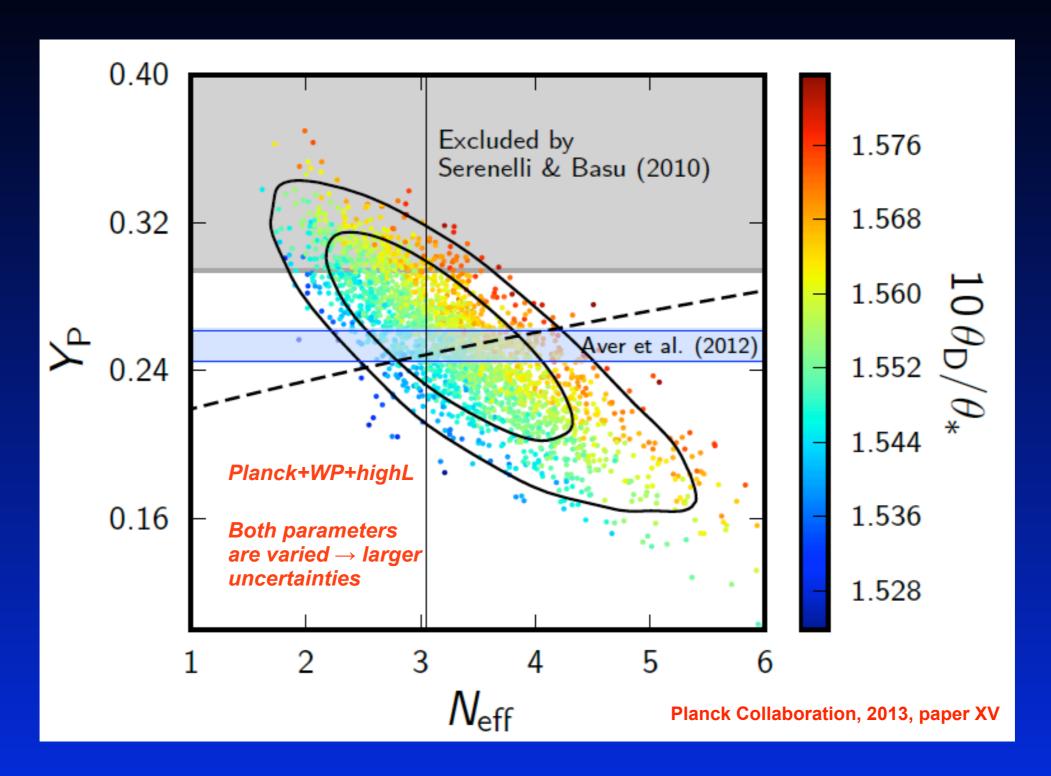
Importance of recombination for inflation constraints



Planck Collaboration, 2015, paper XX

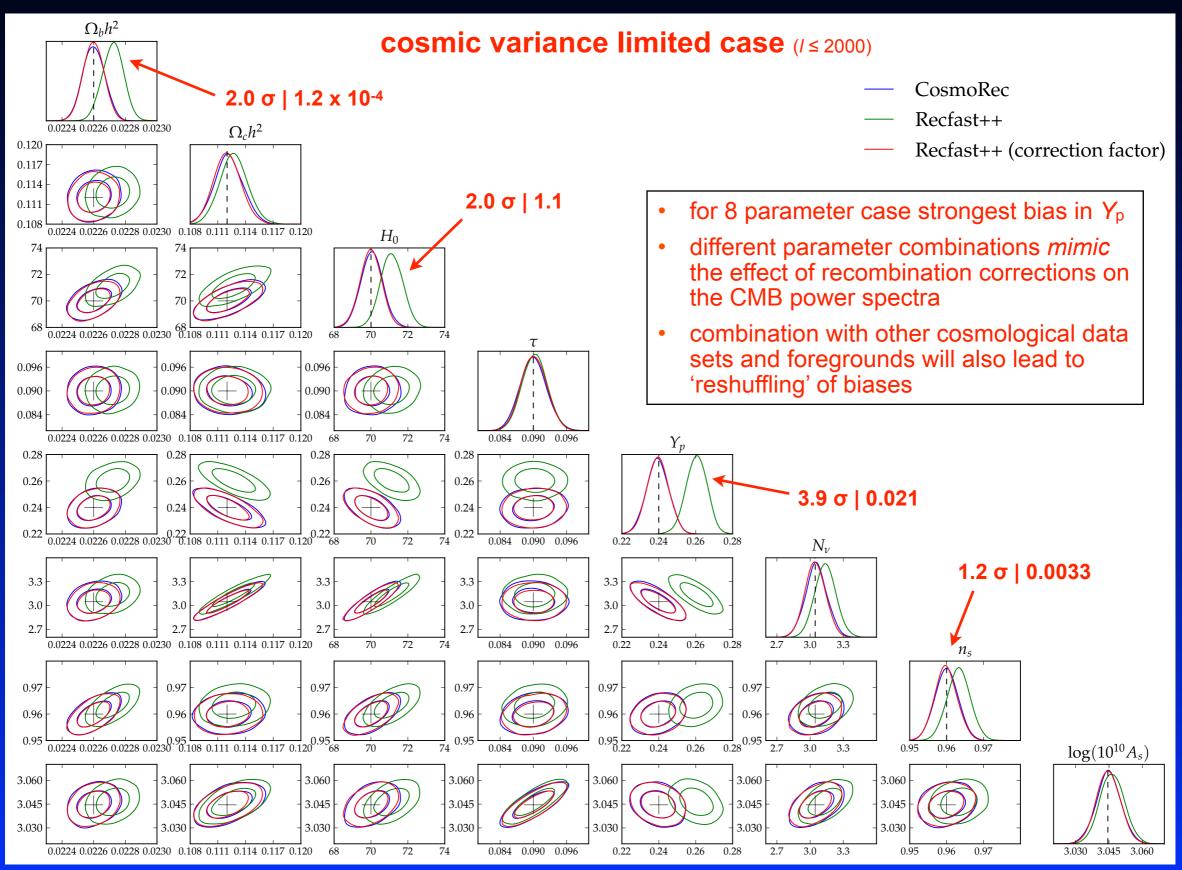
Analysis uses refined recombination model (CosmoRec/HyRec)

CMB constraints on N_{eff} and Y_{p}

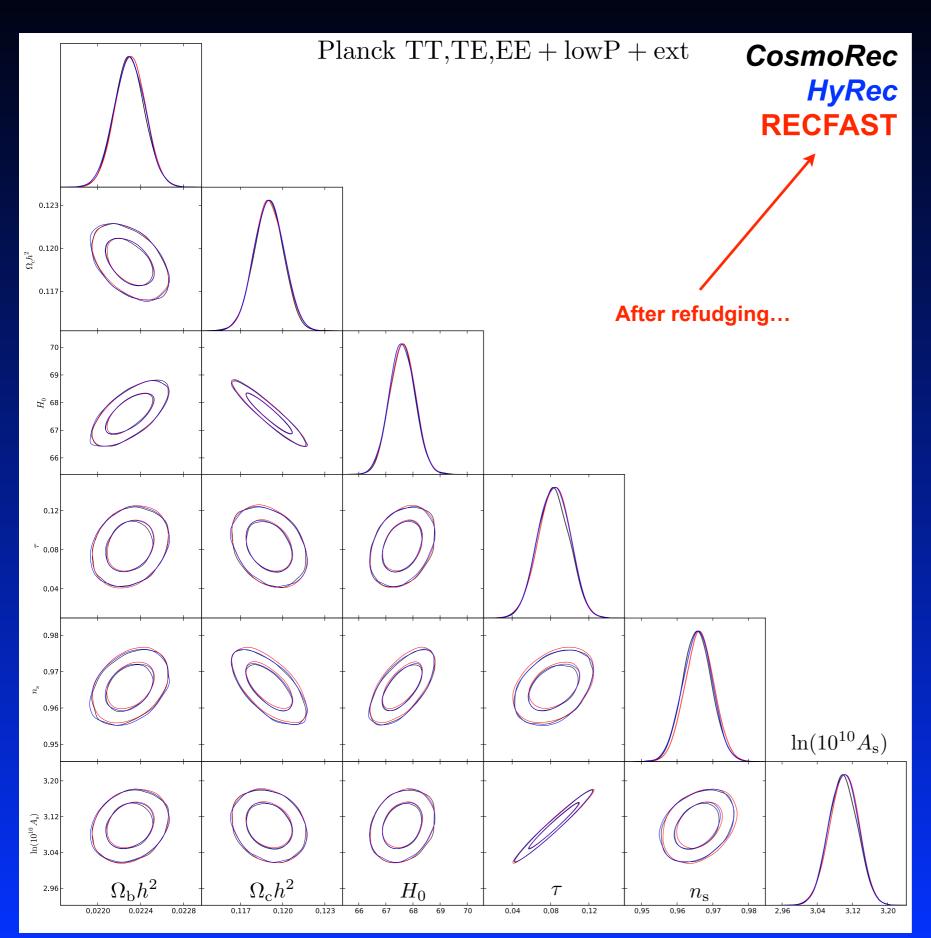


- Consistent with SBBN and standard value for N_{eff}
- Future CMB constraints (Stage-IV CMB) on Yp will reach 1% level

Importance of recombination for measuring helium



Differences for current recombination codes



- Different codes agree very well!
- largest biases

 $\Delta n_{\rm s} \approx 0.15\sigma$ (CosmoRec \Leftrightarrow RECFAST)

 $\Delta n_{\rm s} \approx 0.03\sigma$ (CosmoRec \Leftrightarrow HyRec)

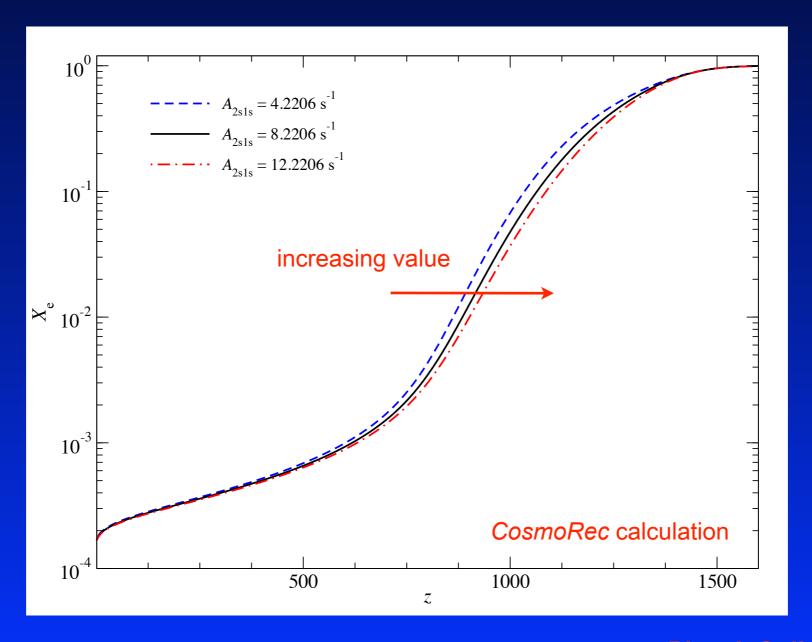
Nothing to worry about at this point!

Planck Collaboration, XIII 2015

Constraints on possible departures from standard recombination history

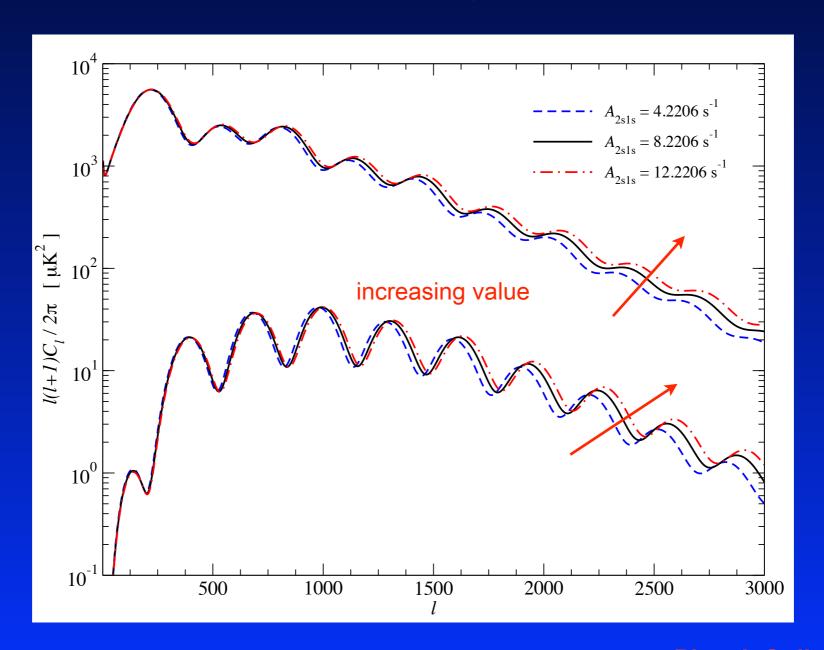
Planck measurement of the HI 2s-1s two-photon rate

- HI 2s-1s two-photon rate crucial for recombination dynamics
- Value is not well measured in lab (best constraint ~ 43% error; Krueger & Oed 1975)
- Planck data can be used to directly constrain its value



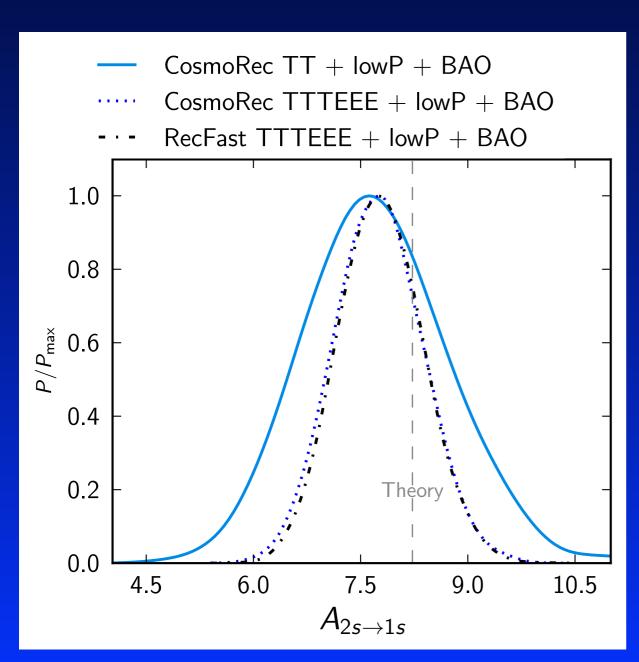
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$$A_{2s\to 1s}^{\text{theory}} = 8.2206 \,\text{s}^{-1}(\text{Labzowsky et al. } 2005)$$

$$A_{2s\rightarrow 1s} = 7.71 \pm 0.99 \,\mathrm{s}^{-1}$$

($Planck \,\mathrm{TT} + \mathrm{lowP} + \mathrm{BAO}$)

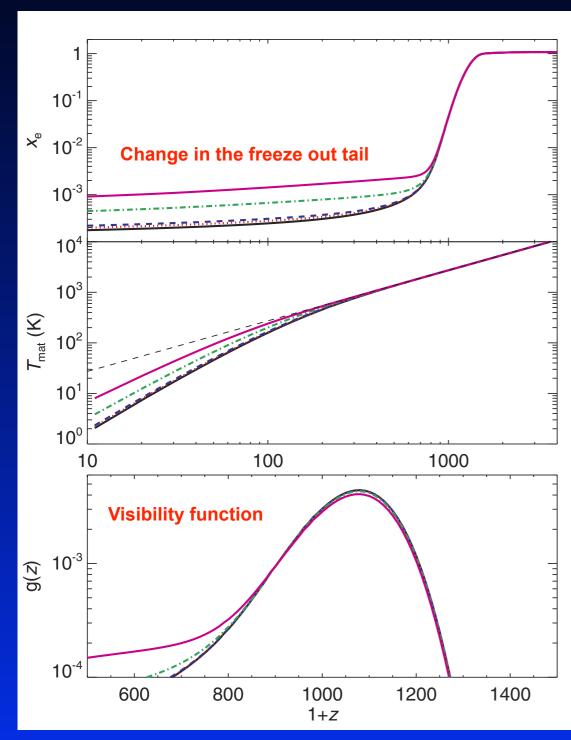
$$A_{2s\rightarrow 1s} = 7.75 \pm 0.61 \,\mathrm{s}^{-1}$$
 ~ 8% errorl
($Planck \,\mathrm{TT,TE,EE+lowP+BAO}$)

- Planck measurement in excellent agreement with theoretical value
- Planck only values very similar
- CosmoRec and Recfast agree...

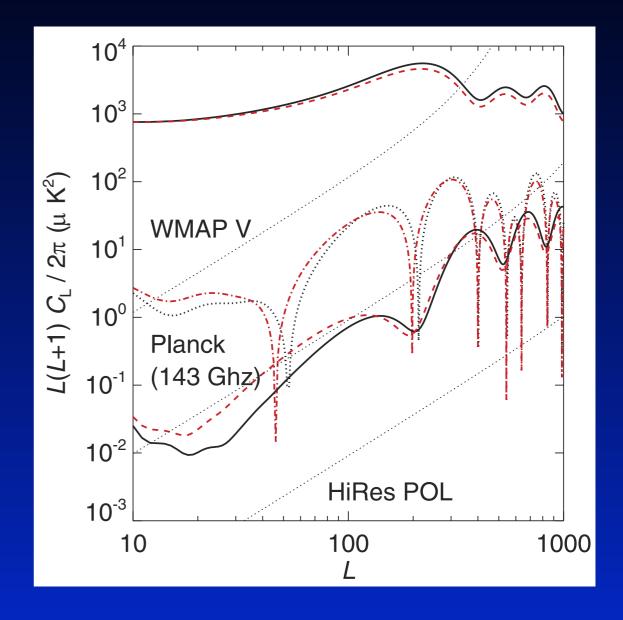


Changes of CMB anisotropies by annihilating particles

95% c.l.



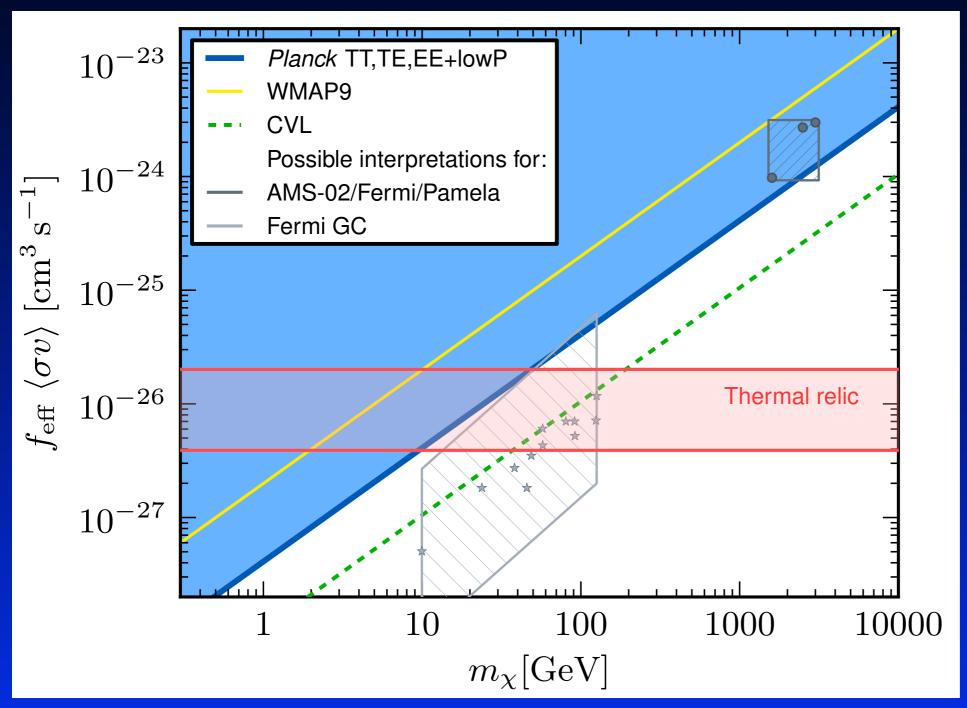
Chen & Kamionikowski, 2004 Padmanabhan & Finkbeiner, 2005



- more damping because τ increases
- change close to visibility maximum → shift in peak positions

Latest Planck limits on annihilation cross section

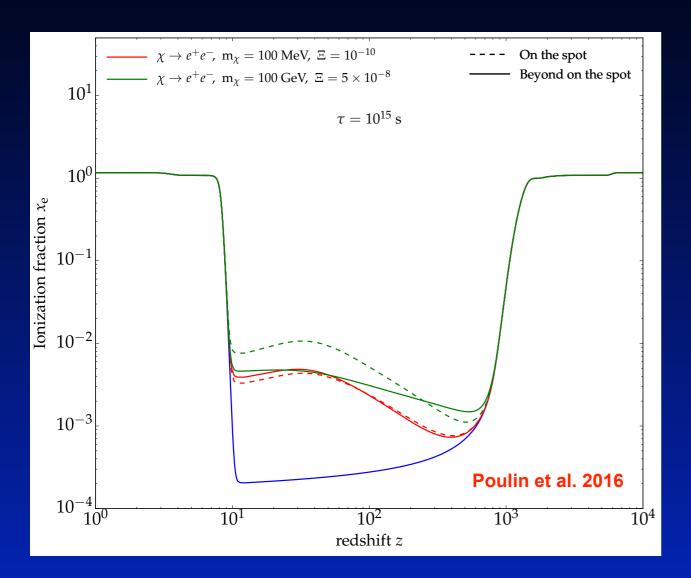
95% c.l.

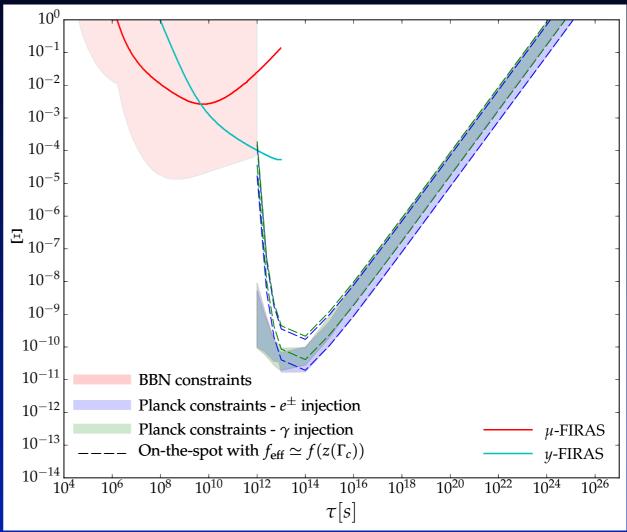


- AMS/Pamela models in tension
- but interpretation model-dependent
- Sommerfeld enhancement?
- clumping factors?
- annihilation channels?

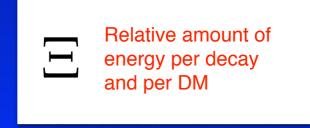
Planck Collaboration, paper XIII, 2015

Effect of decaying particles



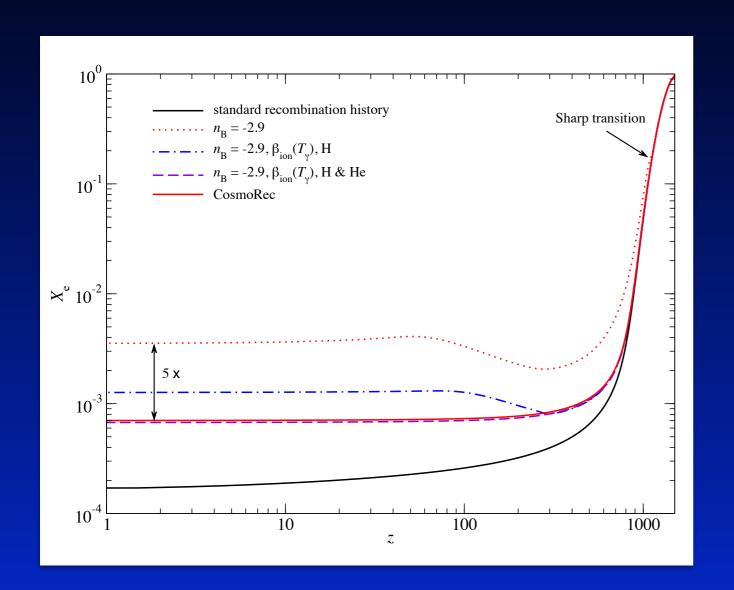


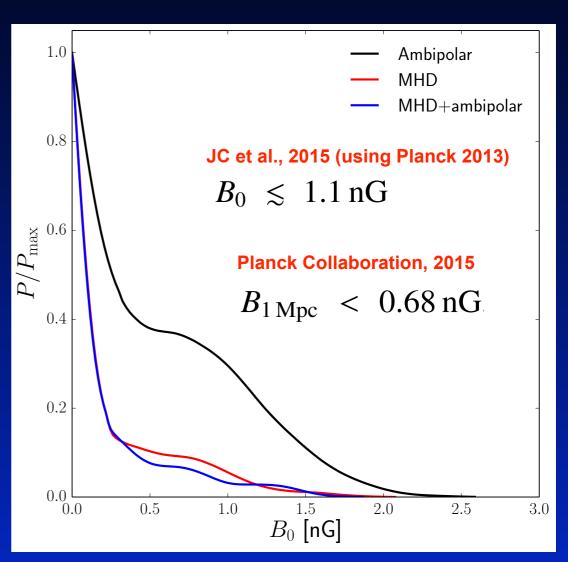
- Effect at different stages of the evolution
- CMB Anisotropies for long-lived particles
- CMB spectral distortions for short-lived particles
- PBHs are similar to decaying particles



Primordial magnetic fields

Changes to recombination from PMFs

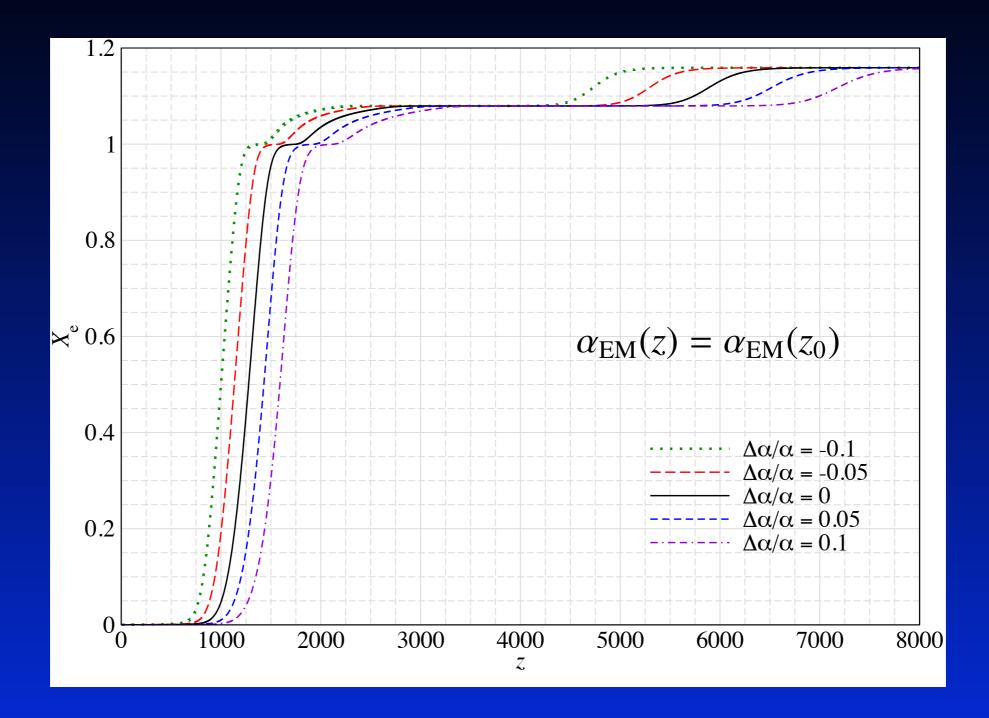




- One has to be careful how to compute the effect...
- Large uncertainties in the heating rates → already working on it....
- Constraints from this effect better than other CMB effects

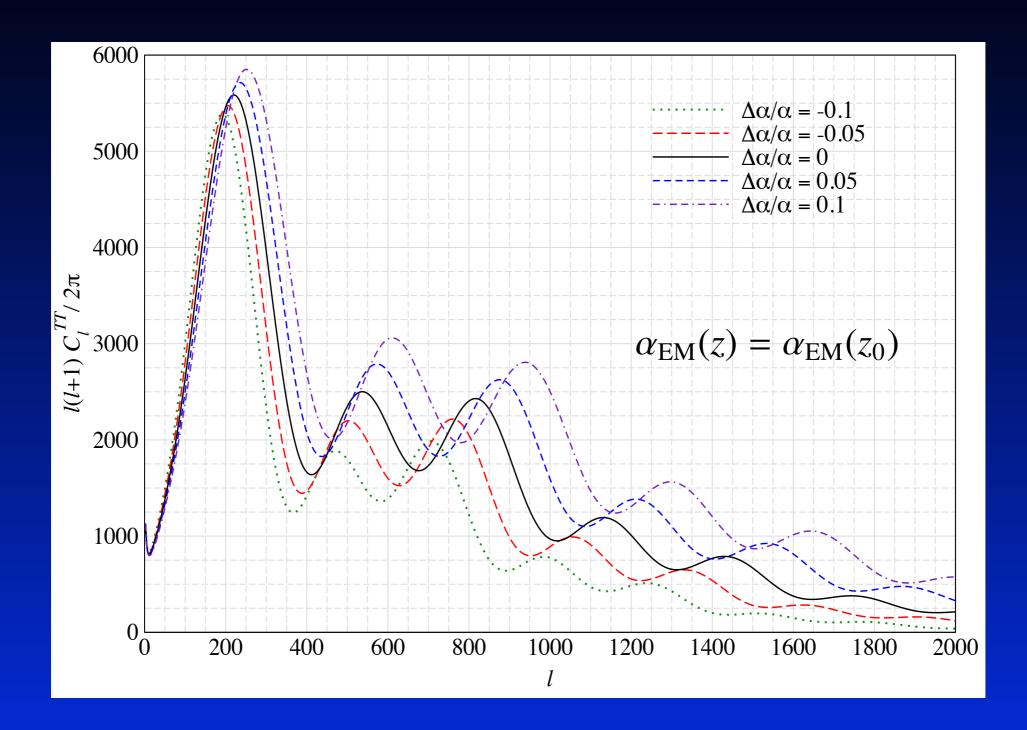
Variations of fundamental constants

Varying the fine-structure constants at recombination



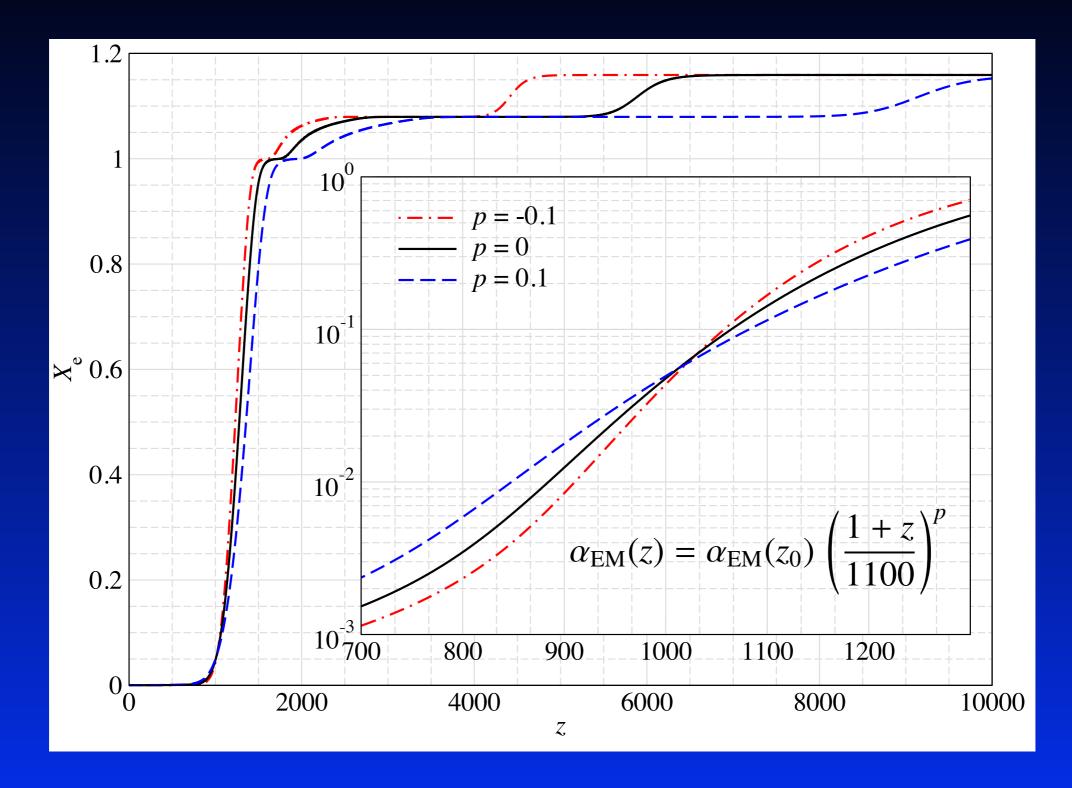
• Constant change of α and m_e were frequently considered (e.g., Kaplinghat et al., 1999; Battye et al., 2001; Planck Collaboration, 2015)

Varying the fine-structure constants at recombination



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Varying the fine-structure constants at recombination



 Data also sensitive to explicit time-dependence around recombination (Luke Hart & JC, 2017)

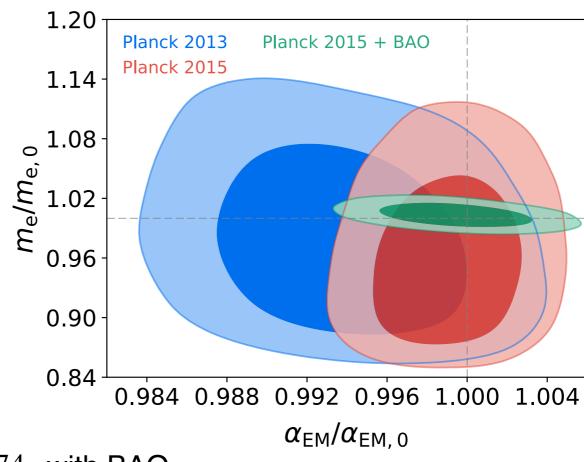
Current constraints using Planck 2015

Parameter	Planck 2015	+ varying $\alpha_{\rm EM}/\alpha_{\rm EM,0}$	+ varying p	+ varying $\alpha_{\rm EM}/\alpha_{\rm EM,0}$ and p
$\Omega_{\rm b} h^2$	0.02224 ± 0.00016	0.02225 ± 0.00016	0.02226 ± 0.00018	0.02223 ± 0.00019
$\Omega_{ m c} h^2$	0.1193 ± 0.0014	0.1191 ± 0.0018	0.1194 ± 0.0014	0.1193 ± 0.0020
$100\theta_{\mathrm{MC}}$	1.0408 ± 0.0003	1.0398 ± 0.0035	1.0408 ± 0.0003	1.0406 ± 0.0051
au	0.062 ± 0.014	0.063 ± 0.014	0.062 ± 0.014	0.063 ± 0.015
$\ln(10^{10}A_{\rm s})$	3.057 ± 0.025	3.060 ± 0.027	3.058 ± 0.026	3.059 ± 0.027
n_{S}	0.9649 ± 0.0047	0.9668 ± 0.0081	0.9663 ± 0.0060	0.9666 ± 0.0081
$\alpha_{\mathrm{EM}}/\alpha_{\mathrm{EM},0}$	_	0.9993 ± 0.0025	_	0.9998 ± 0.0036
p	_	_	0.0008 ± 0.0025	0.0007 ± 0.0036
$H_0 [{\rm km s^{-1} Mpc^{-1}}]$	67.5 ± 0.6	67.2 ± 1.0	67.5 ± 0.6	67.3 ± 1.4

- For α, Planck 2015 gives slight improvement over Planck 2013 because of polarization (~30%)
- Constraint on m_e asymmetric

$$m_{\rm e}/m_{\rm e,0} = 0.961^{+0.046}_{-0.072}$$

 BAO improves m_e constraint and allows breaking degeneracies between α and m_e

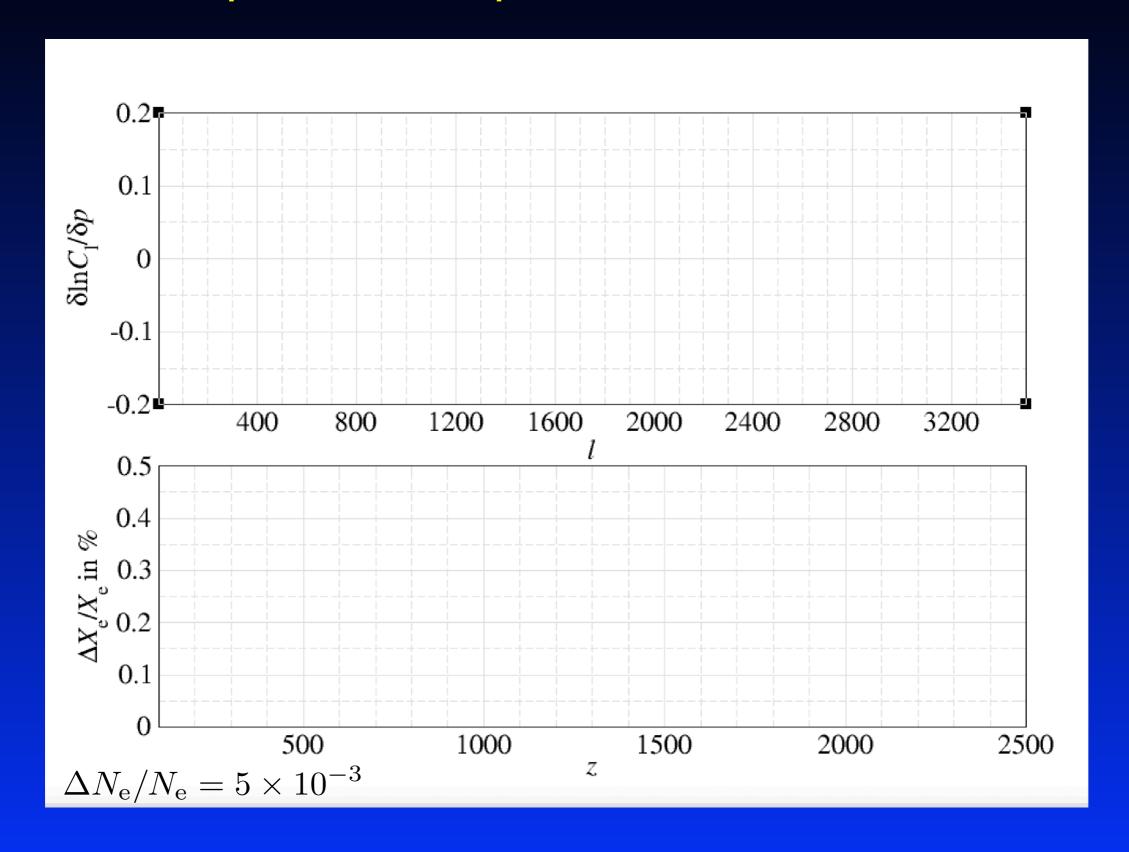


Model-independent constraints

Principle component analysis for recombination

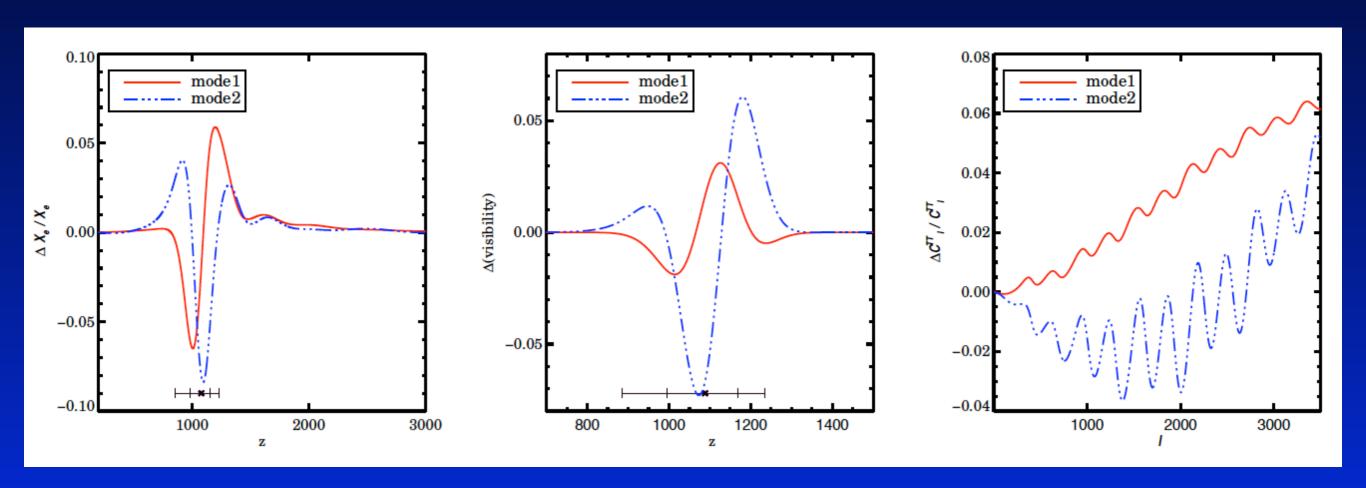
- E.g., something standard was missed, or something non-standard happened !?
- A non-parametric estimation of possible corrections to the recombination history would be very useful → Principle component analysis (PCA)

Power spectrum response at different redshifts

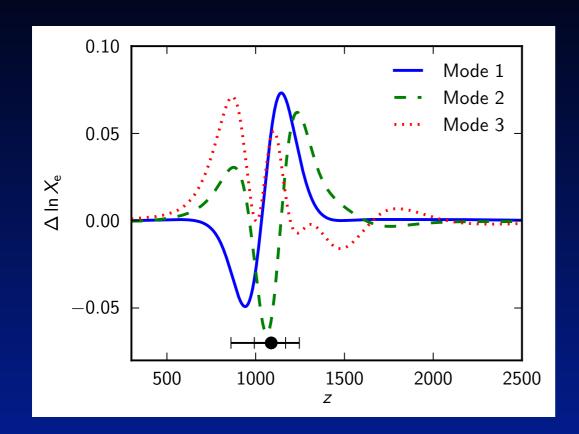


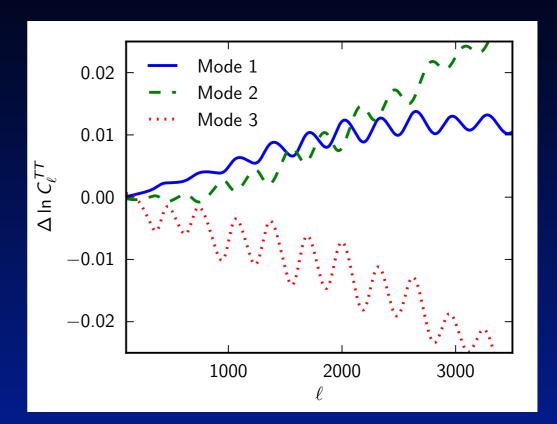
Principle component analysis for recombination

- E.g., something standard was missed, or something non-standard happened!?
- A non-parametric estimation of possible corrections to the recombination history would be very useful → Principle component analysis (PCA)



PCA analysis with Planck 2015

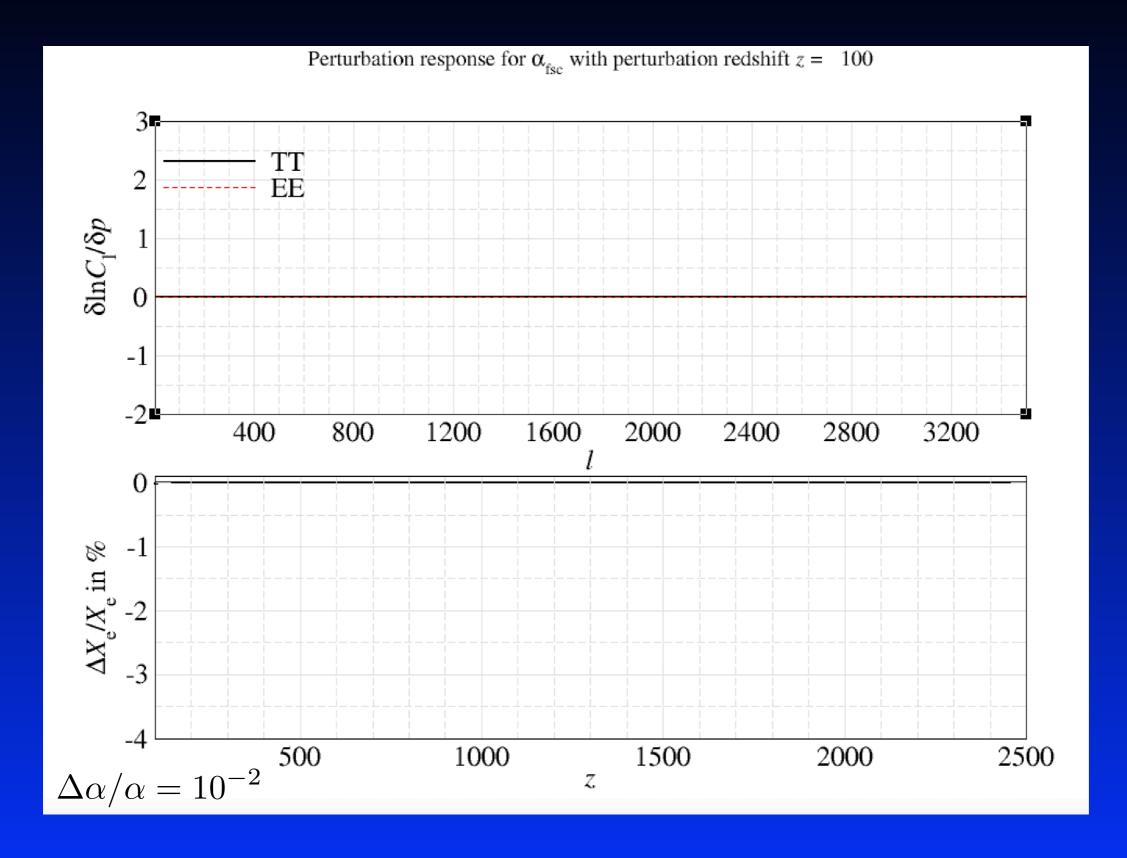




- Planck data is consistent with standard recombination
- Non-trivial statement, even if it is expected!
- Improvement in next release

Parameter	+ 1 mode	+ 2 modes	+ 3 modes
$\Omega_{\rm b}h^2$	0.02229 ± 0.00017	0.02237 ± 0.00018	0.02237 ± 0.00019
$\Omega_{\rm c} h^2 \ldots \ldots$	0.1190 ± 0.0010	0.1186 ± 0.0011	0.1187 ± 0.0012
H_0	67.64 ± 0.48	67.80 ± 0.51	67.80 ± 0.56
τ	0.065 ± 0.012	0.068 ± 0.013	0.068 ± 0.013
$n_{\rm S}$	0.9667 ± 0.0053	0.9677 ± 0.0055	0.9678 ± 0.0067
$\ln(10^{10}A_{\rm s})$	3.062 ± 0.023	3.066 ± 0.024	3.066 ± 0.024
μ_1	-0.03 ± 0.12	0.03 ± 0.14	0.02 ± 0.15
μ_2		-0.17 ± 0.18	-0.18 ± 0.19
μ_3	•••	•••	-0.02 ± 0.88

We can do this for fundamental constants too...

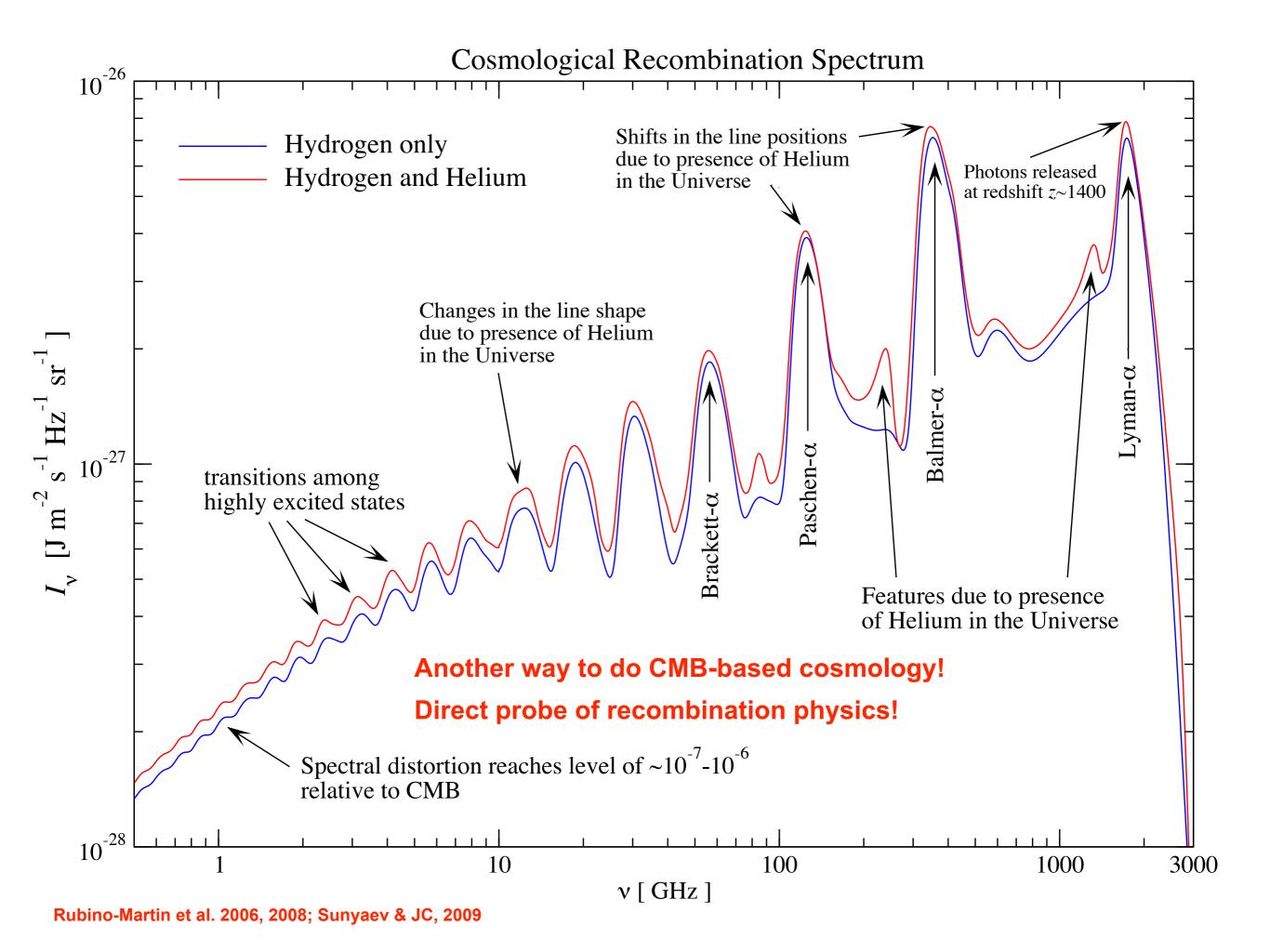


Cosmological Recombination Radiation

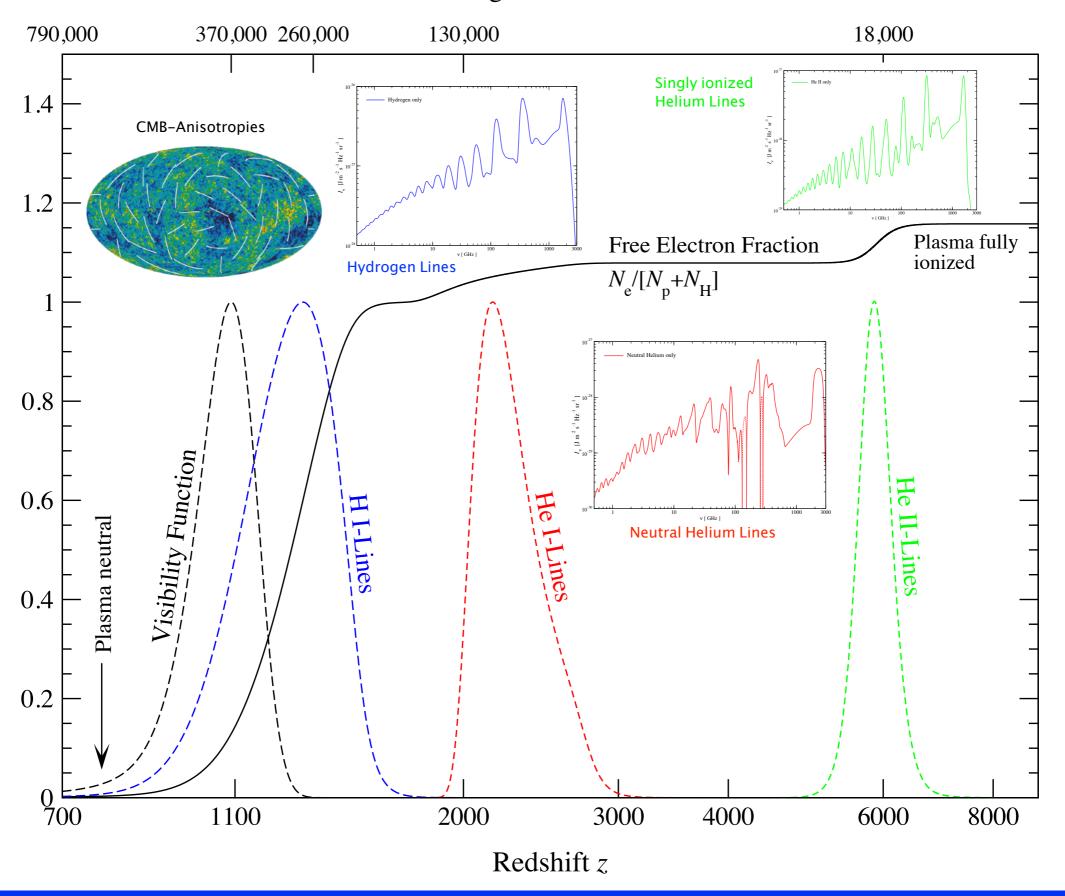
Simple estimates for hydrogen recombination

Hydrogen recombination:

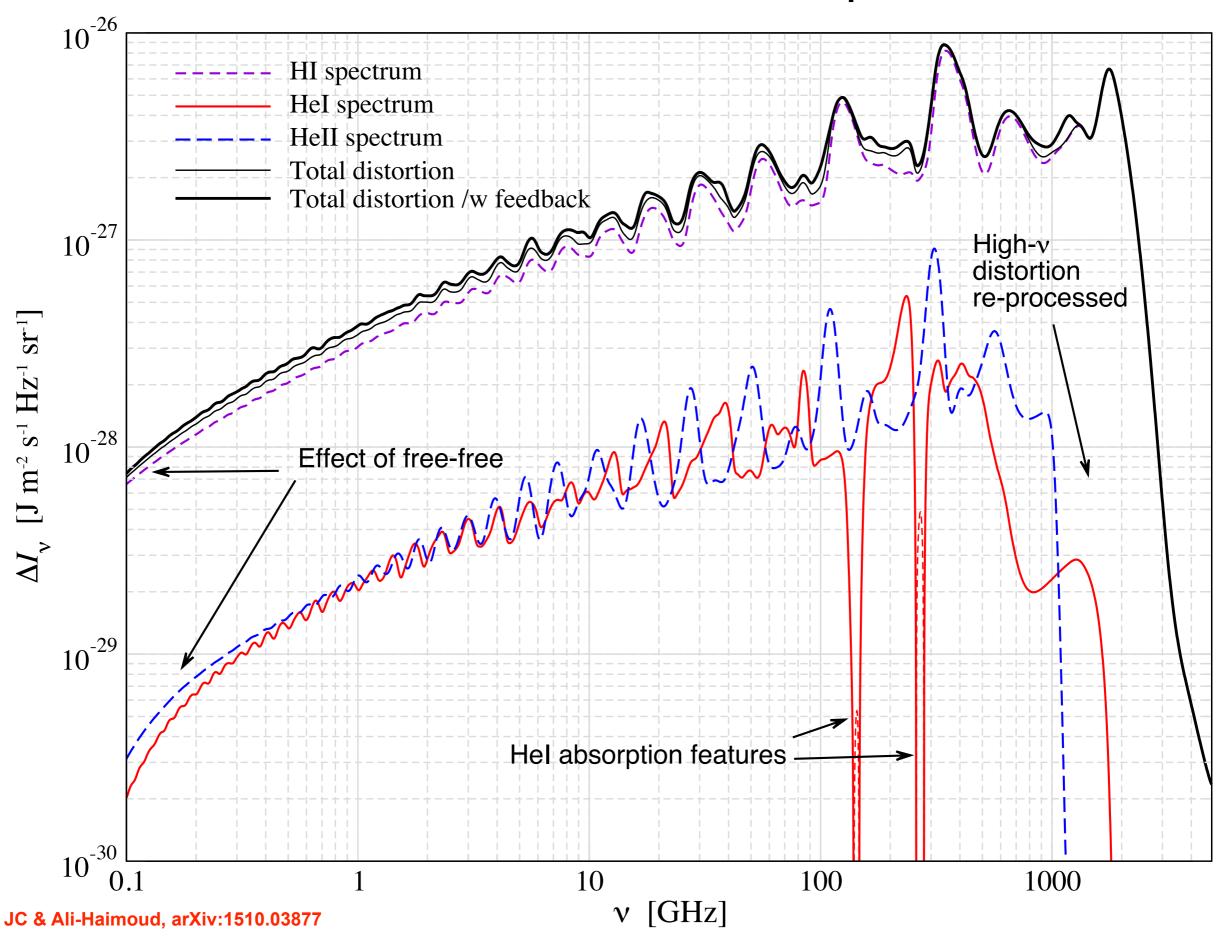
- per recombined hydrogen atom an energy of ~ 13.6 eV in form of photons is released
- at z ~ 1100 $\rightarrow \Delta \epsilon / \epsilon$ ~ 13.6 eV $N_{\rm b}$ / $(N_{\rm y} 2.7 {\rm k} T_{\rm r})$ ~ 10-9 -10-8
- \rightarrow recombination occurs at redshifts $z < 10^4$
- → At that time the *thermalization* process doesn't work anymore!
- There should be some small spectral distortion due to additional Ly-α and 2s-1s photons!
 (Zeldovich, Kurt & Sunyaev, 1968, ZhETF, 55, 278; Peebles, 1968, ApJ, 153, 1)
- In 1975 *Viktor Dubrovich* emphasized the possibility to observe the recombinational lines from n > 3 and $\Delta n << n!$



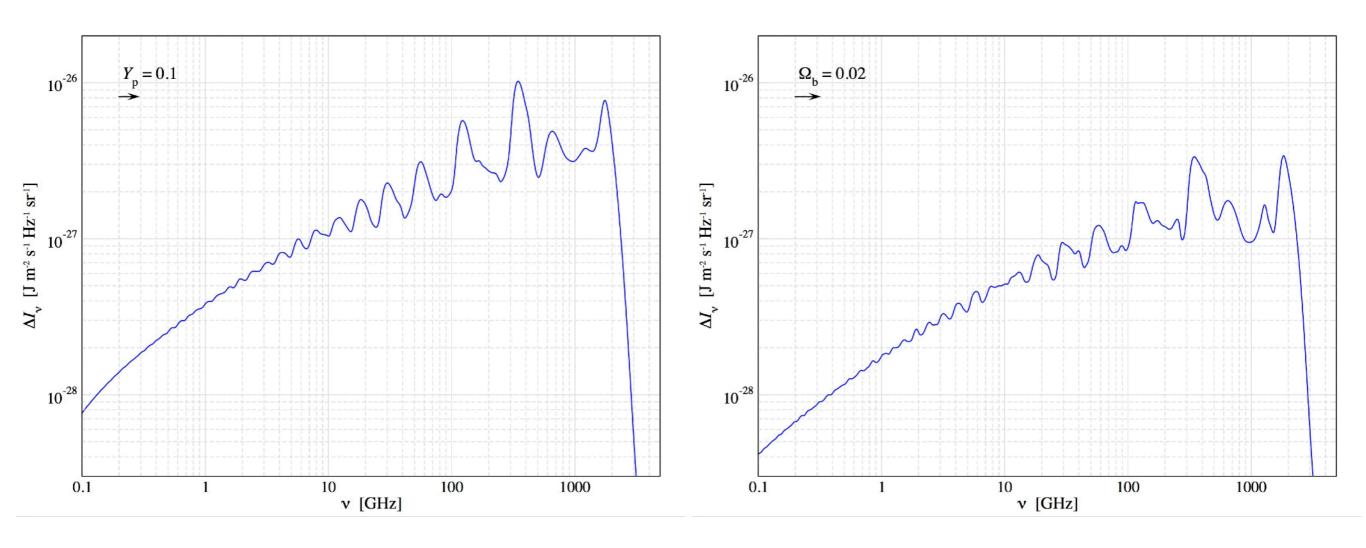
Cosmological Time in Years



New detailed and fast computation!



CosmoSpec: fast and accurate computation of the CRR

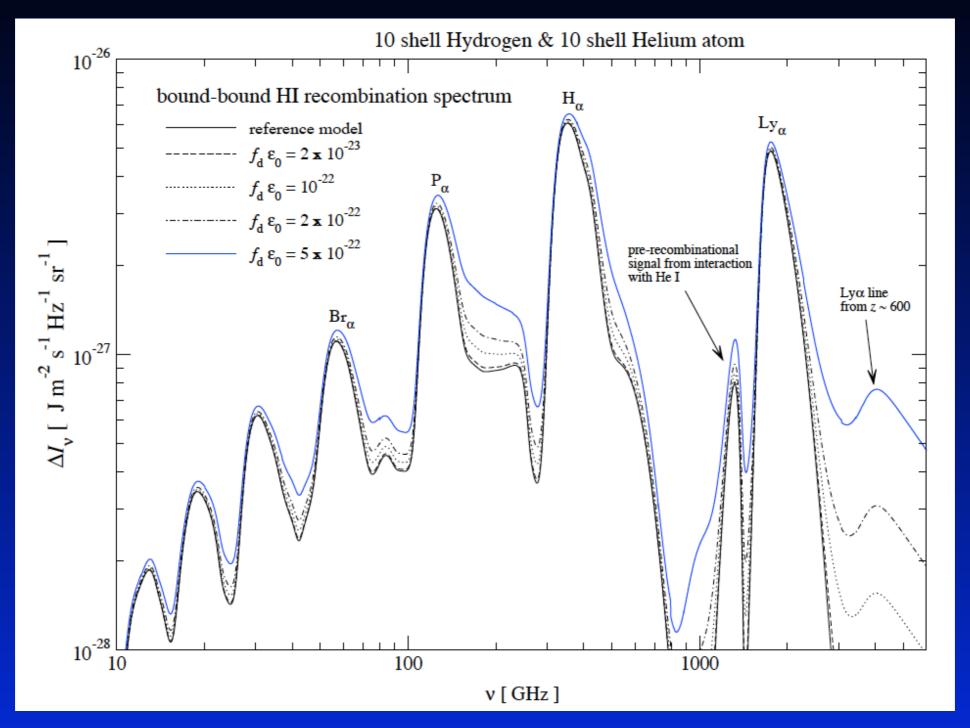


- Like in old days of CMB anisotropies!
- detailed forecasts and feasibility studies
- non-standard physics (variation of α, energy injection etc.)

CosmoSpec will be available here:

www.Chluba.de/CosmoSpec

Dark matter annihilations / decays



- Additional photons at all frequencies
- Broadening of spectral features
- Shifts in the positions

JC, 2009, arXiv:0910.3663

Conclusions

- The standard recombination problem has been solved to a level that is sufficient for the analysis of current and future CMB data (<0.1% precision!)
- Many people helped with this problem!
- Without the improvements over the original version of Recfast cosmological parameters derived from Planck would be biased significantly
- In particular the discussion of inflation models would be affected
- Cosmological recombination radiation allows us to directly constrain the recombination history