

Observables and Unobservables in Dark Energy Cosmologies

Kosmologietag

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Relaxes assumptions behind Λ CDM $\left[\begin{array}{l} G_N = 1 \\ 1 \text{ potential } \Psi \end{array} \right]$

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(we talk only about perturbation theory)

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Dark Energy
configuration:

$$Y(k, a) \equiv -\frac{2k^2\Psi}{3\Omega_m\delta_m} = 1.$$

Effective Newton's Constant

$$\eta(k, a) \equiv -\frac{\Phi}{\Psi} = 1$$

Slip parameter

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time- and scale-dependent
Gravitational coupling

2 potentials

to test for Dark Energy...

to test for deviations of

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Normal approach:

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Normal approach:

- assume a parameterization for free functions
- evolve it in a modified code while fitting the data in a model- (parameterization-) dependent way

a step back

**What is observable without
assuming a DE model?**

a step back

Minimal of assumptions:

FLRW universe

$$ds^2 = -(1 + 2\Psi)dt^2 + a^2(t)(1 + 2\Phi)d\mathbf{x}^2$$

Linear bias

$$\delta_{\text{gal}} = b(k, a)\delta_m$$

Matter follow geodesics
and is pressureless

Equivalence principle holds:
no velocity bias

$$\theta_{\text{gal}} \simeq \theta_m$$

a step back

What can we observe?

Linear perturbations

Weak lensing

$$\kappa = \frac{1}{2} \int_0^{\chi_s} k^2 (\Psi - \Phi) W(\chi, \chi_s) d\chi$$

Redshift-space
distortions

$$\delta_{\text{gal}}^z(k, z, \mu) = \delta_{\text{gal}}(k, z) - \mu^2 \frac{\theta_{\text{gal}}(k, z)}{a^2 H}$$

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Galaxies follow geodesics

$$(a^2 \theta_{\text{gal}})' = a^2 H k^2 \Psi$$



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Map out the metric!

a step back

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+ Equivalence
Principle

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What can we observe?

Redshift-space
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$$\delta_{\text{gal}}^z(k, z, \mu) = \delta_{\text{gal}}(k, z) - \mu \frac{2\theta_{\text{gal}}(k, z)}{a^2 H}$$

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+ Continuity
Equation

$$\theta_m = -\delta'_m - 3\Phi'$$

a step back

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Observation of

$$\delta'_m$$

Observables:

 Ψ Φ δ'_m

Observables:

$$\Psi \quad \Phi \quad \delta'_m$$

ratios

Dark Energy Configuration:

$$Y(k, a) \equiv -\frac{2k^2\Psi}{3\Omega_m\delta_m}$$

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Anisotropic-stress is
observable!

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Anisotropic-stress is
observable!

Growth rate and Effective G, not!

Let's see what this can do for us...

Horndeski

$$\mathcal{L}_2 = K(\phi, X),$$

$$\mathcal{L}_3 = -G_3(\phi, X)\square\phi,$$

$$\mathcal{L}_4 = G_4(\phi, X)R + G_{4,X} \left[(\square\phi)^2 - (\nabla_\mu \nabla_\nu \phi)^2 \right],$$

$$\mathcal{L}_5 = G_5(\phi, X)G_{\mu\nu}\nabla^\mu\nabla^\nu\phi - \frac{G_{5,X}}{6} \left[(\square\phi)^3 - 3(\square\phi)(\nabla_\mu\nabla_\nu\phi)^2 + 2(\nabla_\mu\nabla_\nu\phi)^3 \right].$$



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the most general DE theory described by a single degree of freedom

Horndeski

equation of motion + constraints=

$$\eta \left(\frac{\Psi'}{\Psi} \right)' + \eta'' + \frac{\Psi'}{\Psi} \left(\eta \frac{\Psi'}{\Psi} + 2\eta' + \alpha_1 \eta - \alpha_2 \right) + \alpha_1 \eta' + \alpha_3 \eta - \alpha_5 + k^2 (\alpha_4 \eta - \alpha_6) = \alpha_7 \frac{3(1+z)^3 \theta_m}{2H^3 k^2 \Psi}.$$

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only 7 unknown parameters



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By measuring potentials at different scales and redshift slices we can fully constrain this relation without assuming **any parameterization**

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- it is possible to constrain the most general theory for Dark Energy without parameterizing by measurements in different redshifts and scales

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- minimal of assumptions
- identify observable quantities
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$$\Psi \quad \Phi \quad \delta'_m$$

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- it is possible to constrain the most general theory for Dark Energy without parameterizing by measurements in different redshifts and scales

thank you!