

Gluo-dissociation and quasi-free dissociation in the EFT framework

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Nora Brambilla, MAE, Jacopo Ghiglieri, Antonio Vairo. [arxiv:1109.5826]
Quarkonia in deconfined matter, September 28, Acitrezza

Outline

- 1 Motivation
- 2 Gluo-dissociation
- 3 Quasi-free dissociation
- 4 Conclusions

Motivation

What has been found until now using EFTs in Quarkonia?

- EFT provide a systematic way to extract information from the fact that $m_Q \gg \frac{1}{r} \gg E$ in Quarkonia. Computations are easier and it is more difficult to neglect a needed resummation.
- For $T \gg \frac{1}{r} \sim m_D$ we recover the perturbative potential with an imaginary part found by Laine, Philipsen, Romatschke and Tassler (2007).
- For $T \lesssim \frac{1}{r}$ we were able to compute thermal corrections to the binding energies and the decay width.
- For the decay width we found two different mechanism. The breaking of the singlet into an octet due to the absorption of a gluon from the medium and the Landau damping of the gluons that are exchanged between the heavy quarks.

Other approach to quarkonia decay width

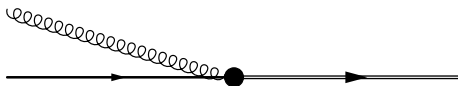
- Use a cross-section computed at $T = 0$, $\sigma(k)$.
- Convolute with the thermal distribution

$$\Gamma = \int \frac{d^3k}{(2\pi)^3} f(k) \sigma(k)$$

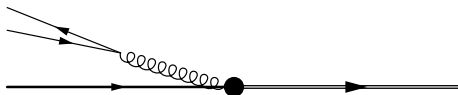
- These cross-sections are computed in perturbation theory and later they are "adapted" to strong coupling by using α_s as a free parameter, introducing thermal masses...
- This information is used as an input to predict the observed suppression in nowadays experiments. See for example Zhao and Rapp (2010).

Perturbative computations of cross-section for quarkonia in the literature

Gluo-dissociation



Bhanot and Peskin (1979)
Quasi-free dissociation



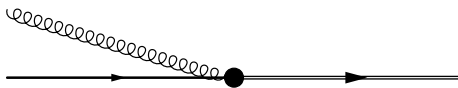
Combridge (1978), Park, Kim, Song, Lee and Wong (2007)

Motivation

- Translate the EFT results that have been found to cross-sections convoluted with distribution function "language".
- Analyze the assumptions made by previous perturbative computations and check if they agree or disagree with the EFT framework.

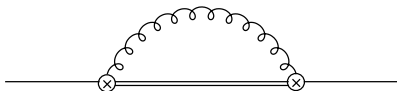
Gluo-dissociation

Gluo-dissociation in Bhanot and Peskin



- They use OPE. The interaction between the singlet, the octet and the gluon is a color dipole interaction.
- This approximation is convenient because the gluo-dissociation is the dominant dissociation mechanism only for $E \gg m_D$. It is very similar to what is done in pNRQCD.
- They use the large N_c limit approximation. In this limit $V_o = 0$ and computations are simplified.
- We are going to see that the large N_c limit is a good approximation for $T \gg E$ but not for $T \sim E$.

Gluo-dissociation in pNRQCD



- Computed for $T \gg E$ in HQ. Brambilla, MAE, Ghiglieri, Soto and Vairo (2010)

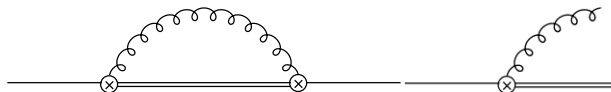
$$\delta\Gamma_n = \frac{1}{3} N_C^2 C_F \alpha_s^3 T - \frac{16}{3m} C_F \alpha_s T E_n + \frac{4}{3} N_C C_F \alpha_s^2 T \frac{2}{mn^2 a_0}$$

where E_n is the binding energy and a_0 the Bohr radius.

- Computed for $T \sim E$ in the hydrogen atom. MAE and Soto (2008).

$$\delta\Gamma_n = \frac{4}{3} \alpha_s C_F T \langle n | r_i \frac{|E_n - h_o|^3}{e^{\beta|E_n - h_o|} - 1} r_i | n \rangle$$

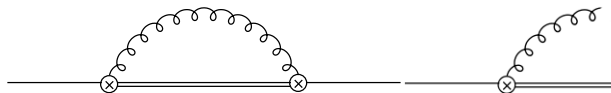
Cutting rules at zero temperature



The imaginary part of the diagram in the left-hand side is related to square of the matrix element in the right-hand side integrated for all the possible phase-space.

In this case at $T = 0$ this decay is not possible due to energy conservation (the phase-space is 0), so the imaginary part of the diagram is 0.

Cutting rules at finite temperature

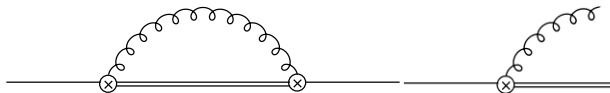


Similar to what is found at $T = 0$.

- Multiply by $n_B(k)$ ($n_F(k)$) for in-coming bosons (fermions).
- Multiply by $1 + n_B(k)$ ($1 - n_F(k)$) for out-going bosons (fermions).

Kobes and Semenoff (1986)

Cutting rules at finite temperature



Similar to what is found at $T = 0$.

- Multiply by $n_B(k)$ ($n_F(k)$) for in-coming bosons (fermions).
- Multiply by $1 + n_B(k)$ ($1 - n_F(k)$) for out-going bosons (fermions).

In this case we get a structure

$$\delta\Gamma_n = \int \frac{d^3k}{(2\pi)^3} n_B(k) \langle n | h_\sigma(r, p, k) | n \rangle$$

A choice

$$\delta\Gamma_n = \int \frac{d^3k}{(2\pi)^3} n_B(k) \langle n | h_\sigma(r, p, k) | n \rangle$$

- If we integrate out k first we recover the pNRQCD result
- If we choose for example $n = 1S$ and compute the matrix element.

$$\delta\Gamma_{1S} = \int \frac{d^3k}{(2\pi)^3} n_B(k) \sigma_{gd}(k)$$

pNRQCD gluo-dissociation σ_{gd} for $1S$

- If we do the same approximations as Bhanot and Peskin (large N_c limit) we recover their result.
- Without doing this approximation we get

$$\sigma_{gd}(k) = \frac{8\pi^2 C_F \alpha_s m a_0^2 k}{3} |\langle 1S | r_i | m a_0^2 (k + E_1) \rangle_o|^2 \Theta(k + E_1)$$

$|\epsilon\rangle_o$ are the octet wave function taking into account the octet potential.

$$\int_0^\infty d\epsilon \langle \epsilon | \epsilon \rangle_o = 1$$

pNRQCD gluo-dissociation σ_{gd} for $1S$

The Coulomb wave-function with a repulsive potential (as the one of the octet) were taken from Abramowitz and Stegun (1972)

$$\sigma_{gd}(k) = \frac{32\pi C_F \alpha_s m a_0^3 k \left(C_1 \left(\frac{1}{8\sqrt{\tau}} \right) \right)^2 \left(f \left(\frac{1}{\sqrt{\tau}} \right) \right)^2}{3\tau^{7/2}} \Theta(\tau)$$

where

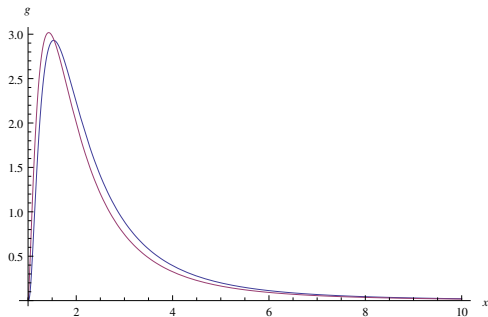
$$\begin{aligned}\tau &= m a_0^2 (k + E_1) \\ C_1(x) &= \frac{\sqrt{1+x^2}}{3} \sqrt{\frac{2\pi x}{e^{2\pi x} - 1}} \\ f(x) &= \frac{51}{2} \frac{x e^{\frac{x}{4} \operatorname{arccot}(x)}}{(x+1)^3}\end{aligned}$$

Agrees with Brezinski and Wolschin (2011)

Comparison between Bhanot and Peskin and pNRQCD gluo-dissociation

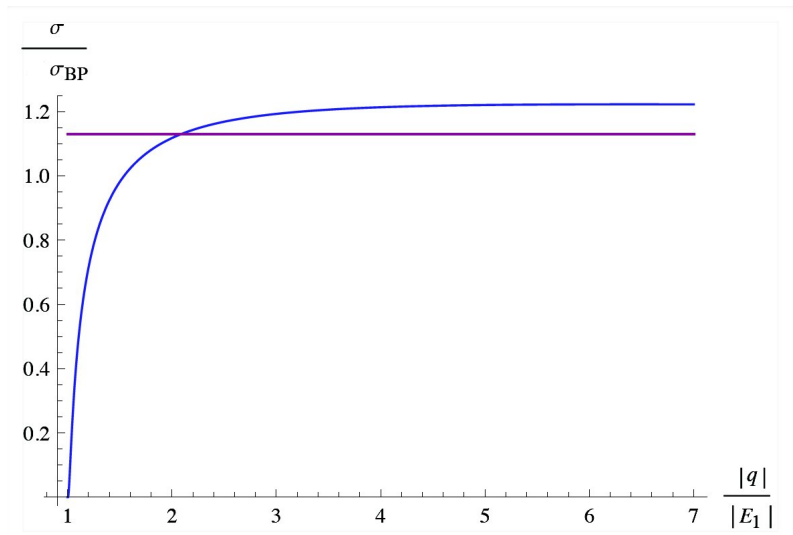
$$\sigma_{gd}(k) = \sigma_R g(x)$$

$$\text{with } \sigma_R = \frac{32\pi C_F \alpha_s a_0^2}{3} \text{ and } x = \frac{k}{|E_1|}$$

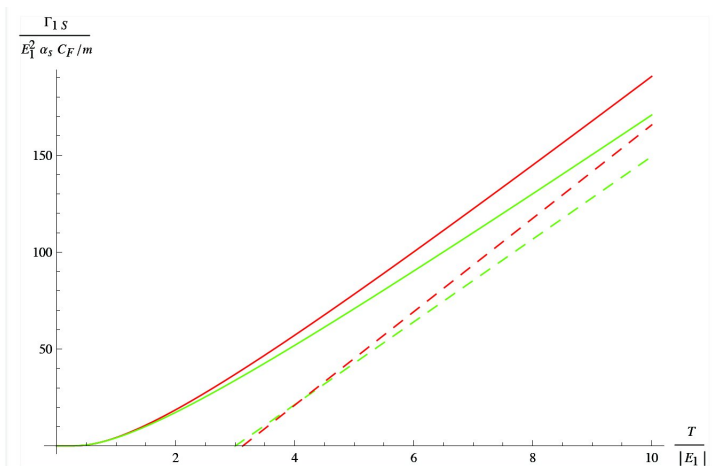


Bhanot and Peskin large N_c limit
pNRQCD

Comparison between Bhanot and Peskin and pNRQCD gluo-dissociation

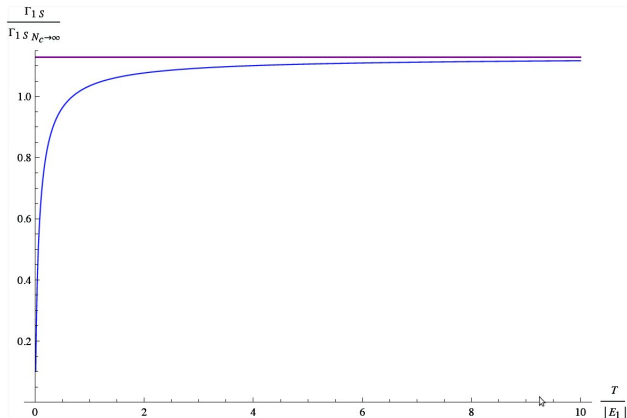


Comparison between Bhanot and Peskin and pNRQCD gluo-dissociation



Bhanot and Peskin, pNRQCD

Comparison between Bhanot and Peskin and pNRQCD gluo-dissociation



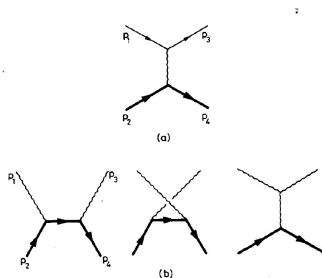
Comparison between Bhanot and Peskin and pNRQCD gluo-dissociation

- In both cases the cross-section goes to 0 for momenta of the gluon bigger than E , so color dipole approximation is justified.
- The decay widths are very different for $T \ll E$, but for this values they are also very small.
- At asymptotically high values of T the ratio tends to the constant $\frac{289}{256}$.

Quasi-free dissociation (Or Landau damping)

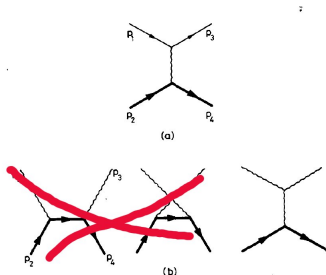
Quasi-free in Cambridge

He computed the process $qc \rightarrow qc$ for a charm quark, no information of the bound state is included.



Quasi-free in Cambridge

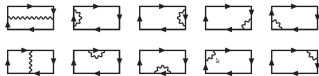
He computed the process $qc \rightarrow qc$ for a charm quark, no information of the bound state is included.



Note that in NRQCD (valid for $m_Q \gg T$) and using the Coulomb gauge the crossed diagrams are subleading.

HQ potential for $T \gg \frac{1}{r} \sim m_D$

Laine, Philipsen, Romatschke and Tassler



pNRQCD



Imaginary part of the potential

$$Im \left(\begin{array}{c} \text{Diagram 1: Two horizontal lines with a wavy loop on top} \\ \text{Diagram 2: Two horizontal lines with a wavy loop on bottom} \\ \text{Diagram 3: Two horizontal lines with a vertical wavy line in the middle} \end{array} \right)$$

By the optical theorem

$$\begin{aligned} & \left| \begin{array}{c} \text{Diagram 1} \\ \text{Diagram 2} \end{array} \right|^2 + \left| \begin{array}{c} \text{Diagram 3} \\ \text{Diagram 4} \end{array} \right|^2 = \\ & \left| \begin{array}{c} \text{Diagram 1} \\ \text{Diagram 2} \end{array} \right|^2 + \left| \begin{array}{c} \text{Diagram 3} \\ \text{Diagram 4} \end{array} \right|^2 + 2Re \left(\left(\begin{array}{c} \text{Diagram 1} \\ \text{Diagram 2} \end{array} \right)^* \begin{array}{c} \text{Diagram 3} \\ \text{Diagram 4} \end{array} \right) \end{aligned}$$

Imaginary part of the potential

$$\text{Im} \left(\begin{array}{c} \text{Diagram 1} \\ \text{Diagram 2} \\ \text{Diagram 3} \end{array} \right) = \begin{array}{c} \left| \text{Diagram 1} \right|^2 + \left| \text{Diagram 2} \right|^2 + 2\text{Re} \left(\left(\text{Diagram 1} \right)^* \text{Diagram 2} \right) \\ \uparrow \qquad \qquad \qquad \uparrow \qquad \qquad \qquad \uparrow \\ \text{Diagram 1} \qquad \qquad \qquad \text{Diagram 2} \qquad \qquad \qquad \text{Diagram 3} \end{array}$$

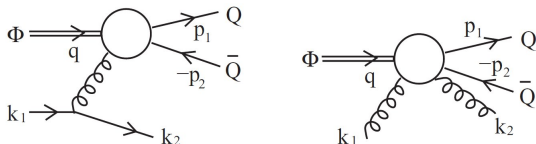
The diagram shows the imaginary part of a sum of three terms. The top row shows the imaginary part of the sum of three diagrams: a diagram with a loop on top, a diagram with a loop on the bottom, and a diagram with a loop on the right. Red arrows point from the bottom row to the top row. The bottom row shows the expansion of the imaginary part of the sum of the first two diagrams, which is the sum of their squared magnitudes plus twice the real part of their product.

Cambridge approximation

$$\text{Im} \left(\begin{array}{c} \text{---} \bullet \text{---} \\ \text{---} \end{array} + \begin{array}{c} \text{---} \\ \text{---} \bullet \text{---} \end{array} + \begin{array}{c} \text{---} \\ \text{---} \end{array} \right)$$
$$\left| \begin{array}{c} \text{---} \\ \text{---} \end{array} \right|^2 + \left| \begin{array}{c} \text{---} \\ \text{---} \end{array} \right|^2 + 2\text{Re} \left(\left(\begin{array}{c} \text{---} \\ \text{---} \end{array} \right)^* \begin{array}{c} \text{---} \\ \text{---} \end{array} \right)$$

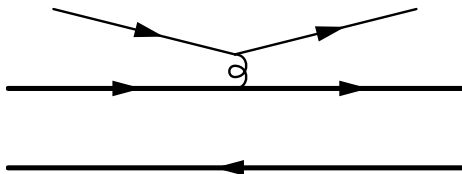
Interference term is neglected. Good approximation for $T, m_D \gg \frac{1}{r}$.

Quasi-free in Park, Kim, Song, Lee and Wong



- For the interaction of the HQ with partons they use vertex computed in Bethe-Salpeter approach and large N_C limit by Song and Lee (2005).
- They assume $q, p_1, p_2 \sim m\alpha_s \gg k_1, k_2$. Their result should be similar to what we got in the $\frac{1}{r} \gg T$ situation.
- They do not give a final analytical cross-section (just the differential one) and include sQGP modelling in the form of thermal masses and binding energies. A real comparison is not possible.

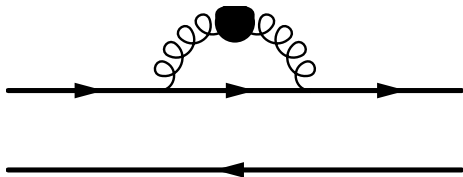
From the cross-section to the decay width



- Apart from the heavy quarks that are not thermalized, there is an in-coming parton and an out-going parton.
- The decay width then has the structure

$$\Gamma = \int \frac{d^3k}{(2\pi)^3} f(k)(1 + f(k))\sigma(k)$$

From the cross-section to the decay width



The information of in-coming and out-going parton is included in EFT formulation in the symmetric self-energy that is included in the gluon propagator (often in the HTL approximation). For example, the part related with fermion loops is

$$\Pi_{00}^S(q \gg q_0) = \frac{4ig^2 T_F N_F}{\pi q} \int_{k > \frac{q}{2}} dk k^2 \left(1 - \frac{q^2}{4k^2}\right) n_F(k)(1 - n_F(k))$$

From the cross-section to the decay width

In conclusion, thermal field theory does not justify in this case

$$\Gamma = \int \frac{d^3k}{(2\pi)^3} f(k)\sigma(k)$$

but instead

$$\Gamma = \int \frac{d^3k}{(2\pi)^3} f(k)(1 + f(k))\sigma(k)$$

Cross-section for the $1S$ state

We proceed in a similar way to what is done for the gluo-dissociation. We start by our previous EFT computations and "translate" them

- In gluo-dissociation only a energy scale was relevant. This is not the case now.
- As we need information of the scale m_D the HTL has to be performed at some part of the computation. σ is going to depend also on the temperature due to this.
- Because we are doing a perturbative computation $T \gg m_D$ which is not the case for quarkonia. However, we still can analyze up to which temperature the color dipole approximation is valid (relation with the Park, Kim, Song , Lee and Wong computation) and at which temperature the Laine et al. potential gives the correct results.

Some notation

$$\sigma(k, m_D) = \sigma_R f(x, y)$$

where

$$\sigma_R = 16\pi C_F \alpha_s^2 T_F N_F a_0^2$$

$$x = m_D a_0$$

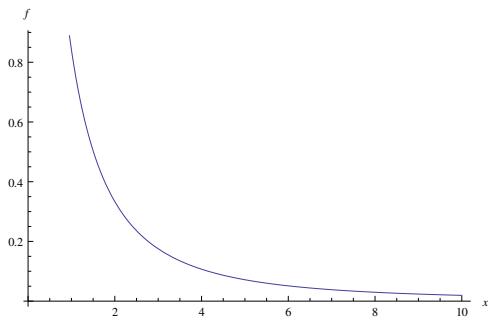
$$y = k a_0$$

I will only show the result for the fermion part, the boson part is quantitatively and qualitatively very similar.

$T \gg \frac{1}{r} \sim m_D$ cross-section for 1S

$$f(x, y) = 2 \left(1 - 4 \frac{x^4 - 16 + 8x^2 \log\left(\frac{4}{x^2}\right)}{(x^2 - 4)^3} \right)$$

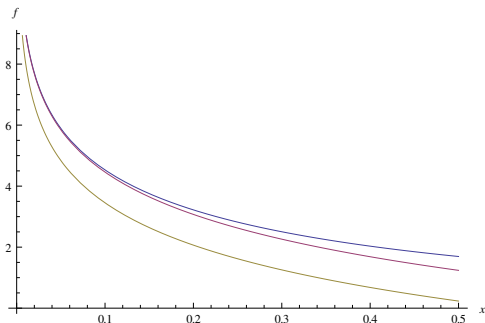
$x \sim 1$ and $y \gg 1$



$T \sim \frac{1}{r} \gg m_D$ cross-section for 1S

$$f(x, y) = -\frac{3}{2} + 2 \log\left(\frac{2}{x}\right) + \log\left(\frac{y^2}{1+y^2}\right) - \frac{1}{y^2} \log(1+y^2)$$

$x \ll 1$ and $y \sim 1$.

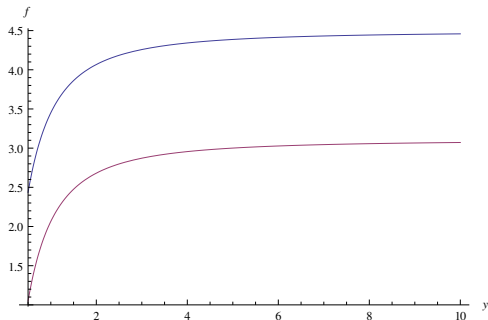


$T \gg \frac{1}{r} \sim m_D$, $ka_0 = 10$ and $ka_0 = 1$. Discrepancy between the blue and red line signals the need for HTL resummation.

$T \sim \frac{1}{r} \gg m_D$ cross-section for 1S

$$f(x, y) = -\frac{3}{2} + 2 \log\left(\frac{2}{x}\right) + \log\left(\frac{y^2}{1+y^2}\right) - \frac{1}{y^2} \log(1+y^2)$$

$x \ll 1$ and $y \sim 1$.

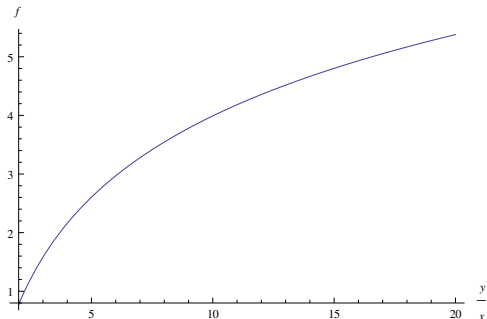


$m_D a_0 = 0.1$ and $m_D a_0 = 0.2$.

$\frac{1}{r} \gg T \gg m_D \gg E$ cross-section for 1S

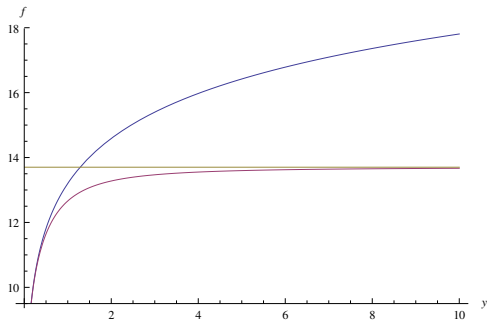
$$f(x, y) = 2 \left(\log \left(\frac{2y}{x} \right) - 1 \right)$$

$1 \gg y \gg x$.



Summary cross-section for 1S

$$m_D a_0 = 0.001$$



$\frac{1}{r} \gg T \gg m_D$, $T \sim \frac{1}{r} \gg m_D$ and $T \gg \frac{1}{r} \sim m_D$. Discrepancy between blue and red lines signals a failure of color dipole approximation.

Gluo-dissociation

- The Bhanot and Peskin result that is normally used correspond to the large N_c limit of pNRQCD result.
- This is a good approximation for $T \gg E$ but it is not so good for $T \sim E$.

Quasi-free dissociation (or Landau damping)

- The imaginary part of the potential and the quasi-free dissociation describe the same physical process at different temperatures.
- The perturbative computations of the cross-section that existed before the use of EFT techniques ignored all bound state properties or used a cross-section equivalent to color dipole approximation.
- Looking at our plots one can see that the color dipole approximation is not so good starting from $Ta_0 \gtrsim 0.3$.
- The quasi-free cross-section goes to an asymptotic value for large incoming momentum. This is the physics described by the imaginary part of Laine et al. potential.

EFT

- Normally one is interested in the Decay width and not in the cross-section. One can obtain this easily with EFTs corrections to potentials and hamiltonians.
- Just using perturbation theory one can not say *a priori* that quasi-free dissociation would be more important than gluo-dissociation for $m_D \gg E$. This piece of information is given by EFT power counting.